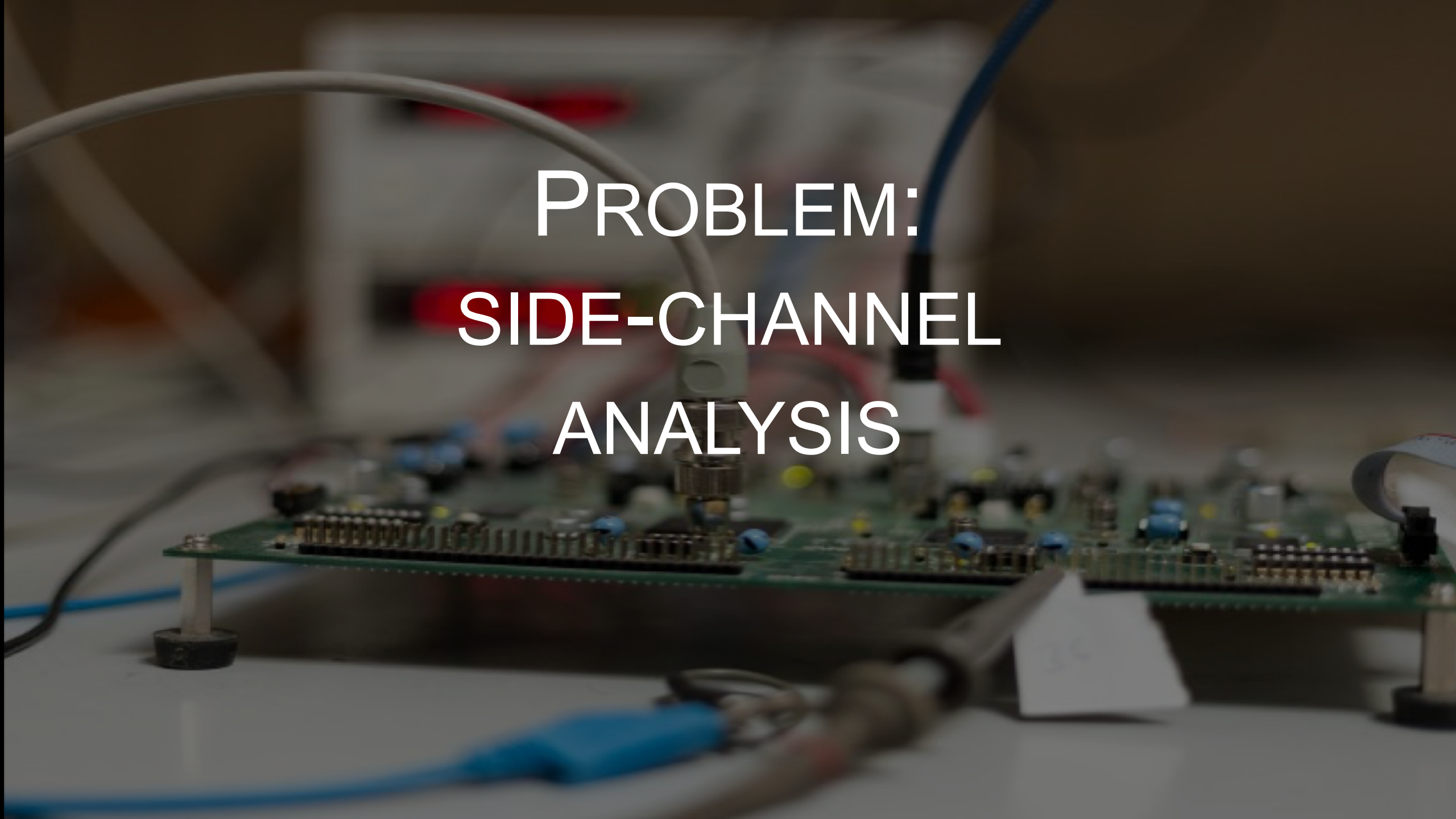




# Consolidating Security Notions in Hardware Masking

CHES 2019

Lauren De Meyer, Begül Bilgin, Oscar Reparaz



PROBLEM:  
SIDE-CHANNEL  
ANALYSIS

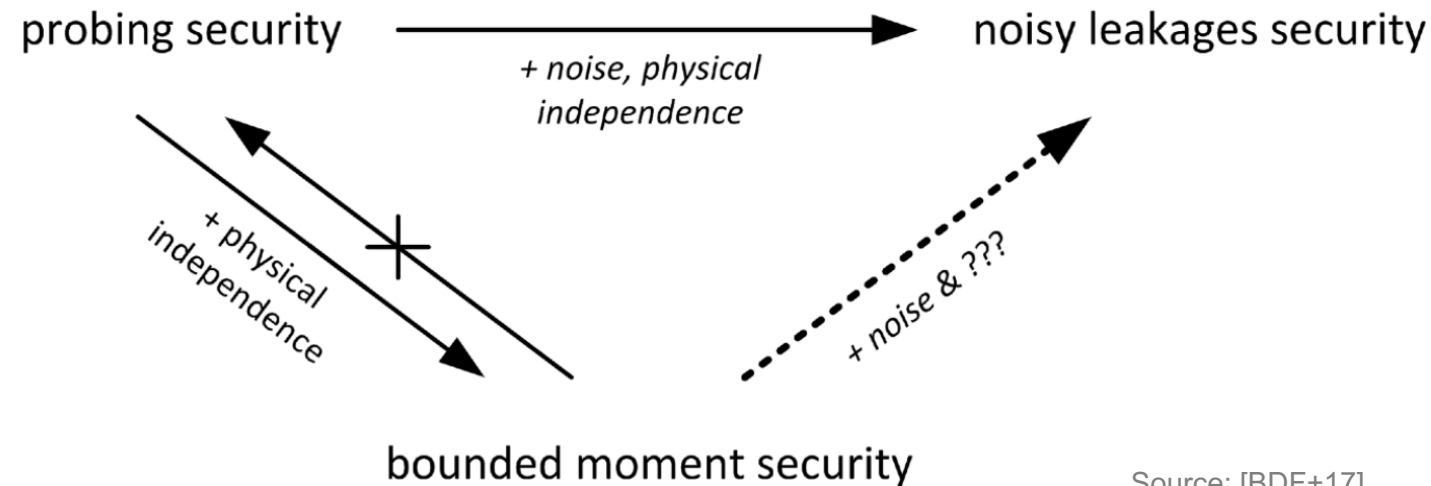
The image shows three men in red jumpsuits and Salvador Dalí masks, a scene from the movie 'Money Heist'. They are standing in a crowd, and the text 'SOLUTION: MASKING' is overlaid in the center. The man in the middle is holding a knife, and the man on the right is holding a gun. The background is a blurred crowd of people.

SOLUTION: MASKING

# PROBING MODEL [ISW03]

- Adversary can probe up to  $d$  intermediate values
- "Ideal circuit": probes are exact and instantaneous and independent

- Basis for many proofs in SCA

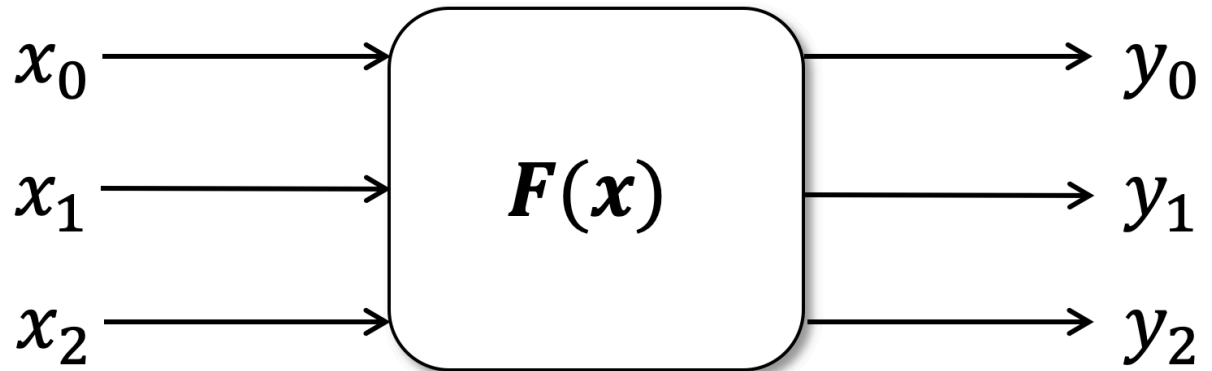


Source: [BDF+17]

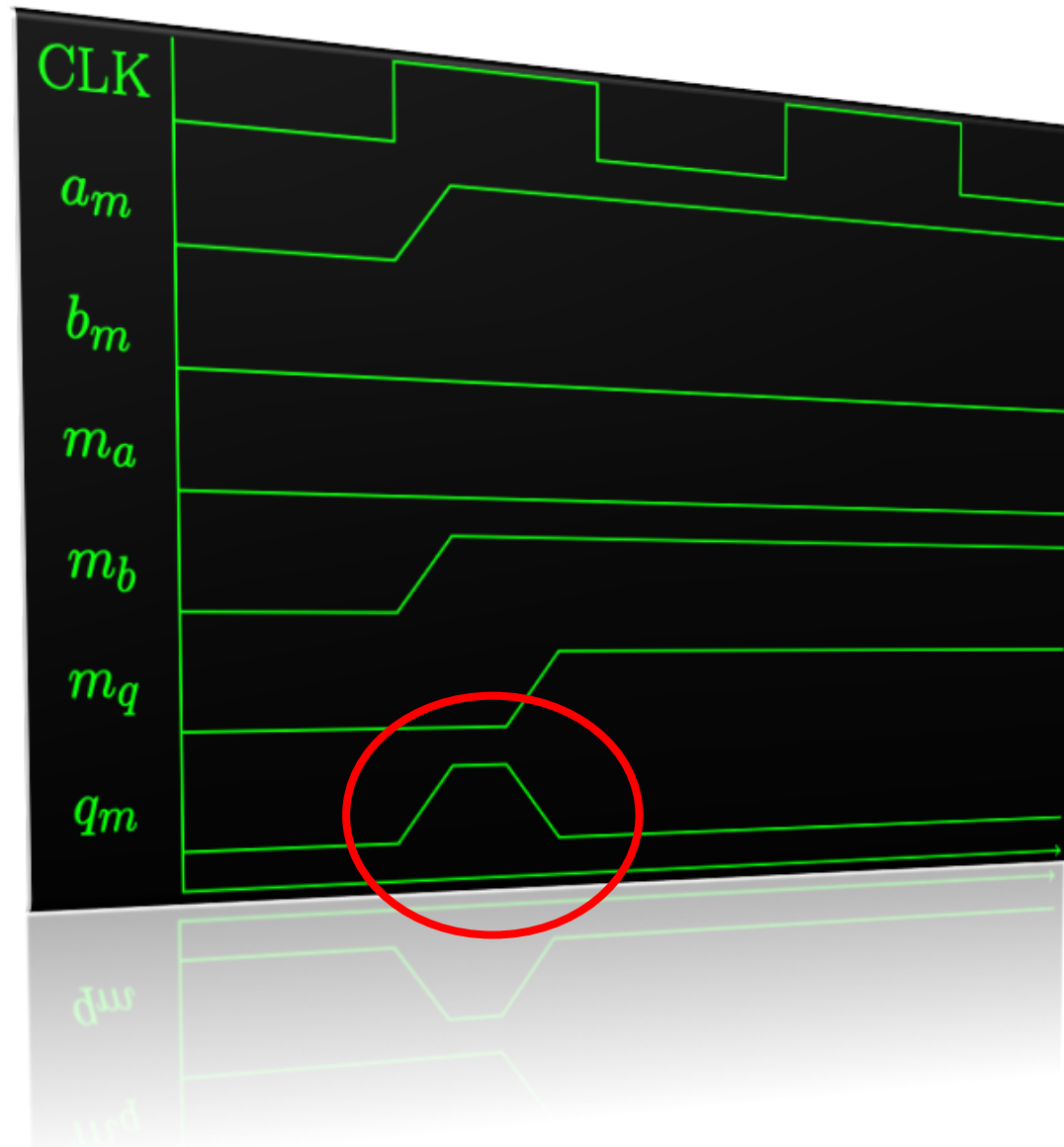


# MASKING

- Goal: no correlation between any  $d$  wires and the secret
- Split sensitive intermediates into  $d + 1$  shares
- $x = x_0 \blacksquare x_1 \blacksquare x_2 \Rightarrow y = F(x) = y_0 \blacksquare y_1 \blacksquare y_2$

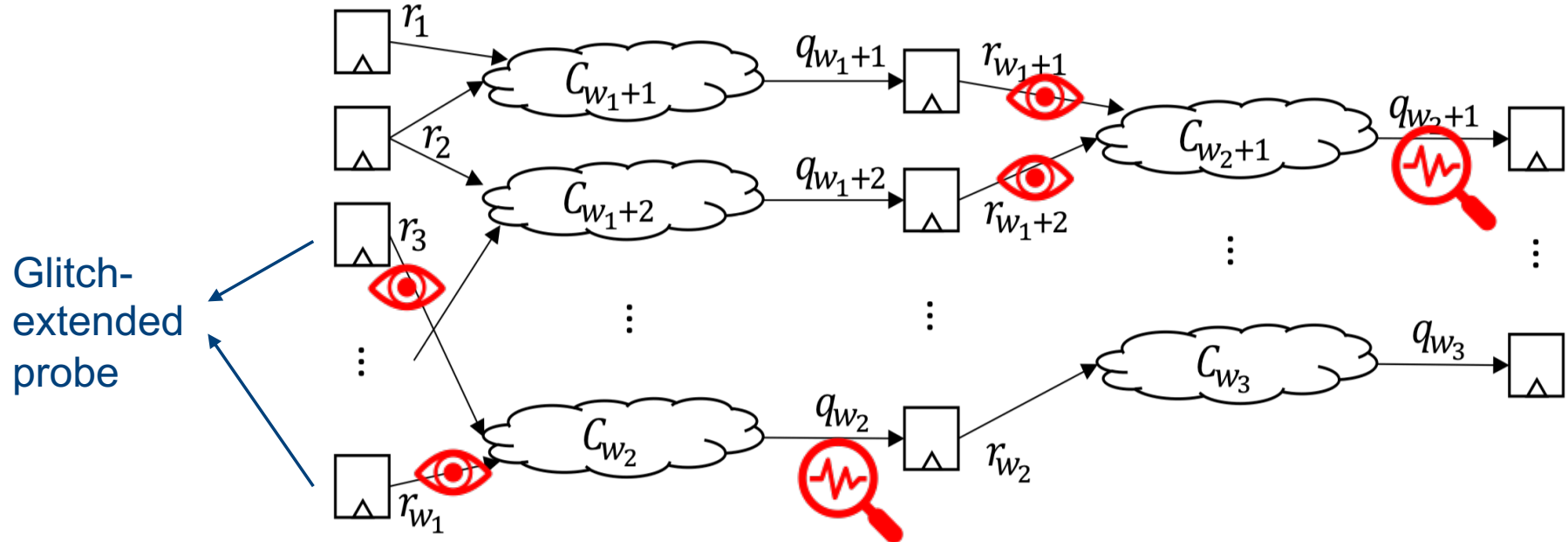


# EXTRA PROBLEM IN HW: GLITCHES!



# GLITCH-EXTENDED PROBING MODEL [RBN+15]

- $d$  probes
- Assume a glitch on combinational logic  $C_i$  can reveal any of its inputs
- → Includes worst-case glitch



$$I(\ ; ) = 0$$





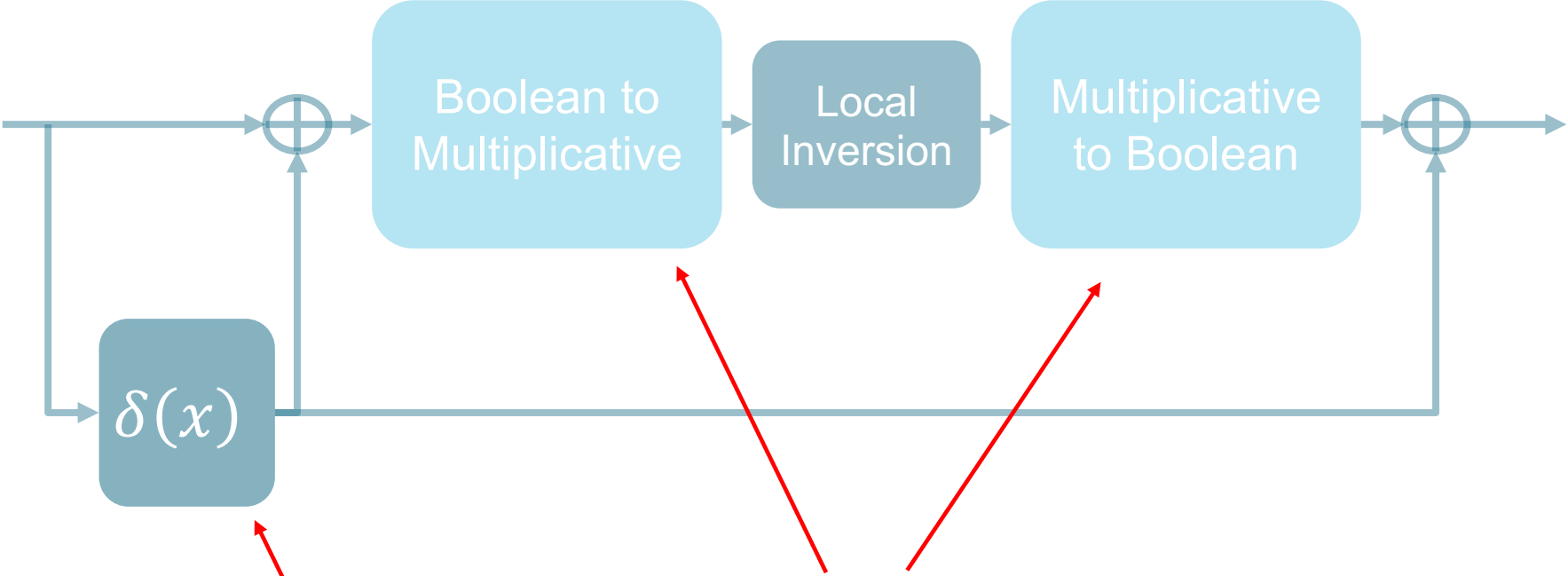
$$I(\cdot; \cdot) = 0$$

- Simple
- Versatile
  - Probing/NI/SNI
  - Different models (with/without glitches, ...)
  - Any type of masking (Boolean, multiplicative, arithmetic, ...)
  - Non-uniformity possible
  - Information-theoretic vs practical security
  - Leakage functions (identity, Hamming, ...)

# THE STORY



# CHES '18: MULTIPLICATIVE MASKING



Randomness recycling

Not Boolean masking

Verification?

# HOW TO VERIFY?

**[1] Probes**

**Multiplicative to Boolean:**  $q_0, q_1, q_2 \in \mathbb{F}_q^*, r_2, r_3, u \stackrel{\$}{\leftarrow} \mathbb{F}_q$

$(b'_0, b'_1) = ((r_3 \oplus u)q_0, (r_2q_1 \oplus u)q_0)$   
 $(b_0, b_2) = ((r_3 \oplus u)q_0, ((q_2 \oplus r_2)q_1 \oplus r_3)q_0)$

$(b'_1, b'_2) = ((r_2q_1 \oplus u)q_0, ((q_2 \oplus r_2)q_1 \oplus r_3)q_0)$   
 $(i_0, b'_0) = (q_2 \oplus r_2, (r_3 \oplus u)q_0)$   
 $(i_1, b'_0) = ((q_2 \oplus r_2)q_1, (r_3 \oplus u)q_0)$   
 $(i_2, b'_0) = (r_2q_1, (r_3 \oplus u)q_0)$   
 $(i_3, b'_0) = (r_3 \oplus u, (r_3 \oplus u)q_0)$   
 $(i_4, b'_0) = ((q_2 \oplus r_2)q_1 \oplus r_3, (r_3 \oplus u)q_0)$   
 $(i_5, b'_0) = ((q_2 \oplus r_2)q_1, (r_2q_1 \oplus u)q_0)$   
 $(i_0, b'_1) = (q_2 \oplus r_2, (r_2q_1 \oplus u)q_0)$   
 $(i_1, b'_1) = (r_2q_1, (r_2q_1 \oplus u)q_0)$   
 $(i_2, b'_1) = (r_3 \oplus u, (r_2q_1 \oplus u)q_0)$   
 $(i_3, b'_1) = ((q_2 \oplus r_2)q_1 \oplus r_3, (r_2q_1 \oplus u)q_0)$   
 $(i_4, b'_1) = (r_2q_1 \oplus u, (r_2q_1 \oplus u)q_0)$   
 $(i_5, b'_1) = (q_2 \oplus r_2, ((q_2 \oplus r_2)q_1 \oplus r_3)q_0)$   
 $(i_0, b'_2) = (q_2 \oplus r_2, ((q_2 \oplus r_2)q_1 \oplus r_3)q_0)$   
 $(i_1, b'_2) = ((q_2 \oplus r_2)q_1, ((q_2 \oplus r_2)q_1 \oplus r_3)q_0)$   
 $(i_2, b'_2) = (r_2q_1, ((q_2 \oplus r_2)q_1 \oplus r_3)q_0)$   
 $(i_3, b'_2) = (r_3 \oplus u, ((q_2 \oplus r_2)q_1 \oplus r_3)q_0)$   
 $(i_4, b'_2) = ((q_2 \oplus r_2)q_1 \oplus r_3, ((q_2 \oplus r_2)q_1 \oplus r_3)q_0)$   
 $(i_5, b'_2) = (r_2q_1 \oplus u, ((q_2 \oplus r_2)q_1 \oplus r_3)q_0)$

$(i_0, i_1) = (q_2 \oplus r_2, (q_2 \oplus r_2)q_1)$   
 $(i_0, i_2) = (q_2 \oplus r_2, r_3 \oplus u)$   
 $(i_0, i_3) = (q_2 \oplus r_2, (q_2 \oplus r_2)q_1 \oplus r_3)$   
 $(i_0, i_4) = (q_2 \oplus r_2, r_2q_1 \oplus u)$   
 $(i_1, i_2) = ((q_2 \oplus r_2)q_1, r_2q_1)$   
 $(i_1, i_3) = ((q_2 \oplus r_2)q_1, r_3 \oplus u)$   
 $(i_1, i_4) = ((q_2 \oplus r_2)q_1, (q_2 \oplus r_2)q_1 \oplus r_3)$   
 $(i_1, i_5) = ((q_2 \oplus r_2)q_1, r_2q_1 \oplus u)$   
 $(i_2, i_3) = (r_2q_1, r_3 \oplus u)$   
 $(i_2, i_4) = (r_2q_1, (q_2 \oplus r_2)q_1 \oplus r_3)$   
 $(i_2, i_5) = (r_2q_1, r_2q_1 \oplus u)$   
 $(i_3, i_4) = (r_3 \oplus u, (q_2 \oplus r_2)q_1 \oplus r_3)$   
 $(i_3, i_5) = (r_3 \oplus u, r_2q_1 \oplus u)$   
 $(i_4, i_5) = ((q_2 \oplus r_2)q_1 \oplus r_3, r_2q_1 \oplus u)$

**Simulation using**

$\sim (r_3q_0, uq_0) \sim (r_3, u)$   
 $\sim (u, r_3q_0) \sim (u, r_3)$   
 $\sim (uq_0, r_3q_0) \sim (r_2, r_3)$   
 $\sim (r_2q_1, r_3q_0) \sim (r_2, r_3)$

$\sim ((q_2 \oplus r_2)q_1 \oplus r_3, uq_0) \sim (r_3, u)$   
 $\sim (r_2q_1 \oplus u, r_3q_0) \sim (u, r_3)$   
 $\sim (q_2 \oplus r_2, uq_0) \sim (r_2, u)$   
 $\sim (r_2q_1, uq_0) \sim (r_2, u)$   
 $\sim ((q_2 \oplus r_2)q_1, uq_0) \sim (r_2, u)$   
 $\sim (r_3, (r_2q_1 \oplus u)q_0) \sim (r_3, uq_0) \sim (r_3, u)$   
 $\sim (r_3, uq_0) \sim (r_3, u)$   
 $\sim (r_3, (r_2q_1 \oplus u)q_0) \sim (r_3, uq_0) \sim (r_3, u)$   
 $\sim (q_2 \oplus r_2, r_3q_0) \sim (r_2, r_3)$   
 $\sim (r_2q_1, r_3q_0) \sim (r_2, r_3)$   
 $\sim ((q_2 \oplus r_2)q_1, r_3q_0) \sim (r_2q_1, r_3q_0) \sim (r_2, r_3)$   
 $\sim (u, ((q_2 \oplus r_2)q_1 \oplus r_3)q_0) \sim (u, r_3)$   
 $\sim (u, r_3q_0) \sim (r_3, r_3)$   
 $\sim (u, ((q_2 \oplus r_2)q_1 \oplus r_3)q_0) \sim (u, r_3)$   
 $\sim (u, r_3q_0) \sim (r_3, r_3)$

**[2] Probes**

**Boolean to multiplicative:**  $b \in \mathbb{F}_q^*, r_0, r_1 \stackrel{\$}{\leftarrow} \mathbb{F}_q^*, u \stackrel{\$}{\leftarrow} \mathbb{F}_q$

$(p_0, p_1) = (r_0, r_1)$   
 $(p_1, p_2) = (r_0, r_1 r_0 b)$   
 $(i_0, p_0) = (r_1, r_1 r_0 b)$   
 $(i_1, p_0) = (r_0 b_0, r_0)$   
 $(i_2, p_0) = (r_0 b_2, r_0)$   
 $(i_3, p_0) = (r_0 b_1, r_0)$   
 $(i_4, p_0) = (r_0 b_0 \oplus r_0 b_1, r_0)$   
 $(i_5, p_0) = (r_0 b_2 \oplus r_0 b_1 \oplus u, r_0)$   
 $(i_6, p_0) = (r_1(r_0 b_0 \oplus r_0 b_2 \oplus u), r_0)$   
 $(i_7, p_0) = (r_1(r_0 b_0 \oplus r_0 b_2 \oplus u), r_0)$   
 $(i_0, p_1) = (r_1(r_0 b_0 \oplus r_0 b_2 \oplus u), r_0)$   
 $(i_1, p_1) = (r_0 b_0, r_1)$   
 $(i_2, p_1) = (r_0 b_2, r_1)$   
 $(i_3, p_1) = (r_0 b_1, r_1)$   
 $(i_4, p_1) = (r_0 b_1 \oplus u, r_1)$   
 $(i_5, p_1) = (r_0 b_2 \oplus r_0 b_1 \oplus u, r_1)$   
 $(i_6, p_1) = (r_1(r_0 b_0 \oplus r_0 b_2 \oplus u), r_1)$   
 $(i_7, p_1) = (r_1(r_0 b_0 \oplus r_0 b_2 \oplus u), r_1)$   
 $(i_0, p_2) = (r_1(r_0 b_0 \oplus r_0 b_2 \oplus u), r_1)$   
 $(i_1, p_2) = (r_0 b_0, r_1 r_0 b)$   
 $(i_2, p_2) = (r_0 b_2, r_1 r_0 b)$   
 $(i_3, p_2) = (r_0 b_1, r_1 r_0 b)$   
 $(i_4, p_2) = (r_0 b_1 \oplus u, r_1 r_0 b)$   
 $(i_5, p_2) = (r_0 b_2 \oplus r_0 b_1 \oplus u, r_1 r_0 b)$   
 $(i_6, p_2) = (r_1(r_0 b_0 \oplus r_0 b_2 \oplus u), r_1 r_0 b)$   
 $(i_7, p_2) = (r_1(r_0 b_0 \oplus r_0 b_2 \oplus u), r_1 r_0 b)$   
 $(i_0, i_1) = (r_0 b_0, r_0 b)$   
 $(i_0, i_2) = (r_0 b_0, r_0 b)$   
 $(i_0, i_3) = (r_0 b_0, r_0 b)$   
 $(i_0, i_4) = (r_0 b_0, r_0 b \oplus u)$   
 $(i_0, i_5) = (r_0 b_0, r_0 b \oplus r_0 b_1 \oplus u)$   
 $(i_0, i_6) = (r_0 b_0, r_0 b \oplus u)$   
 $(i_0, i_7) = (r_0 b_0, r_1(r_0 b_0 \oplus r_0 b_2 \oplus u))$   
 $(i_1, i_2) = (r_0 b_1, r_1(r_0 b_2 \oplus u))$   
 $(i_1, i_3) = (r_0 b_1, r_0 b)$   
 $(i_1, i_4) = (r_0 b_1, r_0 b \oplus u)$   
 $(i_1, i_5) = (r_0 b_1, r_0 b \oplus r_0 b_1 \oplus u)$   
 $(i_1, i_6) = (r_0 b_1, r_0 b \oplus u)$   
 $(i_1, i_7) = (r_0 b_1, r_1(r_0 b_2 \oplus u))$   
 $(i_2, i_3) = (r_0 b_2, r_1(r_0 b_2 \oplus u))$   
 $(i_2, i_4) = (r_0 b_2, r_0 b \oplus u)$   
 $(i_2, i_5) = (r_0 b_2, r_0 b \oplus u)$   
 $(i_2, i_6) = (r_0 b_2, r_0 b \oplus u)$   
 $(i_2, i_7) = (r_0 b_2, r_1(r_0 b_2 \oplus u))$   
 $(i_3, i_4) = (r_0 b_1, r_1(r_0 b_0 \oplus r_0 b_2 \oplus u))$   
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 $(i_3, i_6) = (r_0 b_1, r_0 b \oplus u)$   
 $(i_3, i_7) = (r_0 b_1, r_1(r_0 b_2 \oplus u))$   
 $(i_4, i_5) = (r_0 b_1 \oplus u, r_0 b \oplus u)$   
 $(i_4, i_6) = (r_0 b_0 \oplus r_0 b_1 \oplus u, r_1(r_0 b_2 \oplus u))$   
 $(i_4, i_7) = (r_0 b_0 \oplus r_0 b_1 \oplus u, r_1(r_0 b_2 \oplus u))$   
 $(i_5, i_6) = (r_0 b_2 \oplus r_0 b_1 \oplus u, r_1(r_0 b_2 \oplus u))$   
 $(i_5, i_7) = (r_0 b_2 \oplus r_0 b_1 \oplus u, r_1(r_0 b_2 \oplus u))$   
 $(i_6, i_7) = (r_1(r_0 b_0 \oplus r_0 b_2 \oplus u), r_1(r_0 b_2 \oplus u))$

$\sim (r_0, r_1)$   
 $\sim (r_1, r_0)$

$\sim (u, r_0)$   
 $\sim (r_1 u, r_0)$

$\sim (u, r_1)$   
 $\sim (r_1 u, r_1)$

$\sim (r_0 b_0, r_1)$   
 $\sim (r_0 b_2, r_1)$   
 $\sim (u, r_1)$   
 $\sim (u, r_1)$   
 $\sim (r_1 u, r_0)$   
 $\sim (r_1 u, r_1 r_0 b) \sim (r_1 u, r_0)$

$\sim (r_0 b_2, u)$   
 $\sim (r_0 b_2, r_1 u)$

$\sim (r_0 \oplus u, u)$   
 $\sim (r_0 \oplus u, r_1 u)$

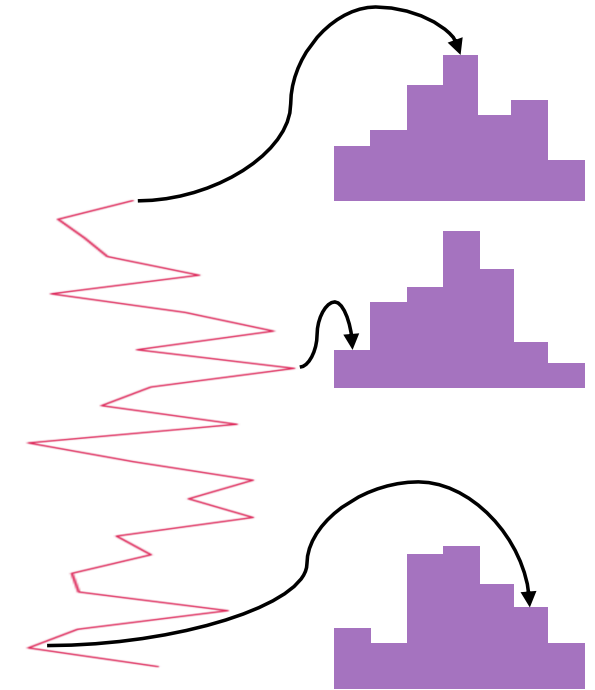
$\sim (r_1(r_0 \oplus u), r_1 u)$



# TOOL FROM [REP16]

```
u8 m1 = nonzero_rnd() & bitmask; add_timesample(m1);  
u8 b1 = crypto_input_shares[0]; add_timesample(b1);  
u8 b2 = crypto_input_shares[1]; add_timesample(b2);  
  
u8 b1m1 = mult_log(b1, m1); add_timesample(b1m1);  
u8 b2m1 = mult_log(b2, m1); add_timesample(b2m1);  
u8 m2 = b1m1 ^ b2m1; add_timesample(m2);
```

0x31  
0x9A  
0xF5  
0x3F  
0xB5  
0x8A



- Simulated traces of intermediates
- Random inputs
- → TVLA (t-test) to detect flaws
- Higher orders: combine probes (e.g. centered product)
- Only for software (no glitches ☹ )

# IDEA: GLITCH-EXTENDED PROBES

```
u8 m1 = nonzero_rnd() & bitmask; add_timesample(m1);  
u8 b1 = crypto_input_shares[0]; add_timesample(b1);  
u8 b2 = crypto_input_shares[1]; add_timesample(b2);  
  
u8 b1m1 = mult_log(b1, m1); add_timesample(b1, m1);  
u8 b2m1 = mult_log(b2, m1); add_timesample(b2, m1);  
u8 m2 = b1m1 ^ b2m1; add_timesample(b1m1, b2m1);
```

0x31

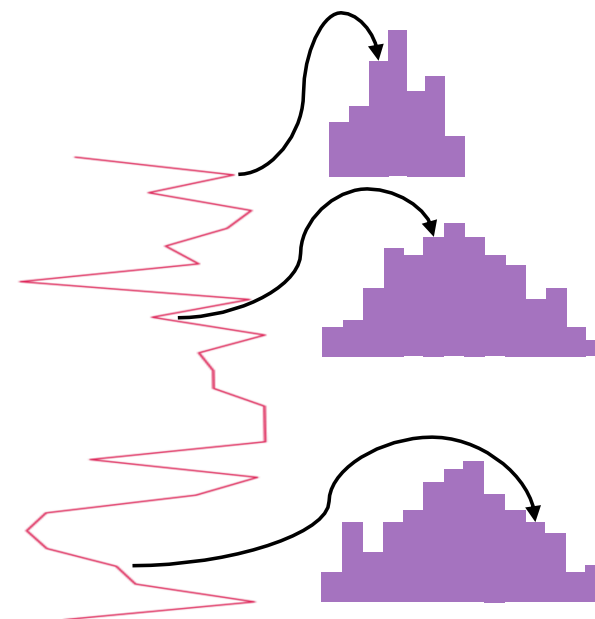
0x9A

0xF5

0x319A

0x31F5

0x3FB5



- Replace regular probes with glitch-extended probes
- → TVLA to detect flaws
- Higher orders: ?



# IDEA: GLITCH-EXTENDED PROBES

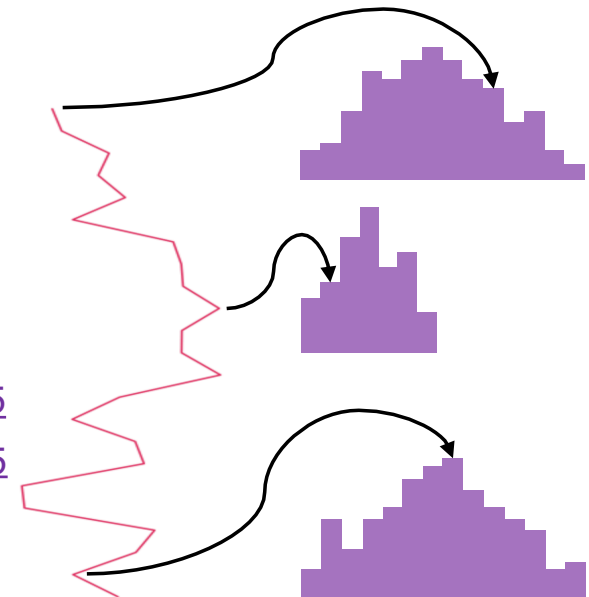
- Higher orders: concatenate extended probes
- $\rightarrow \chi^2$  test to detect flaws

```
u8 m1 = nonzero_rnd() & bitmask; add_timesample(m1);  
u8 b1 = crypto_input_shares[0]; add_timesample(b1);  
u8 b2 = crypto_input_shares[1]; add_timesample(b2);  
  
u8 b1m1 = mult_log(b1, m1); add_timesample(b1, m1);  
u8 b2m1 = mult_log(b2, m1); add_timesample(b2, m1);  
u8 m2 = b1m1 ^ b2m1; add_timesample(b1m1, b2m1);
```

0x9A31F5

0x31F53FB5

0x319A3FB5



ESSENTIALLY:

$$I(\mathcal{R}; x) = 0$$

# PROBING SECURITY WITH/WITHOUT GLITCHES



# PROBING SECURITY [GM10]

*Given  $d$  wires  $Q = (q_1, \dots, q_d)$*

$$I(Q; x) = 0$$

# GLITCH-EXTENDED PROBING SECURITY

*Given  $d$  wires  $Q = (q_1, \dots, q_d)$   
with glitch-extended probes  $\mathcal{R} = (\mathcal{R}_1, \dots, \mathcal{R}_d)$*

$$I(\mathcal{R}; x) = 0$$

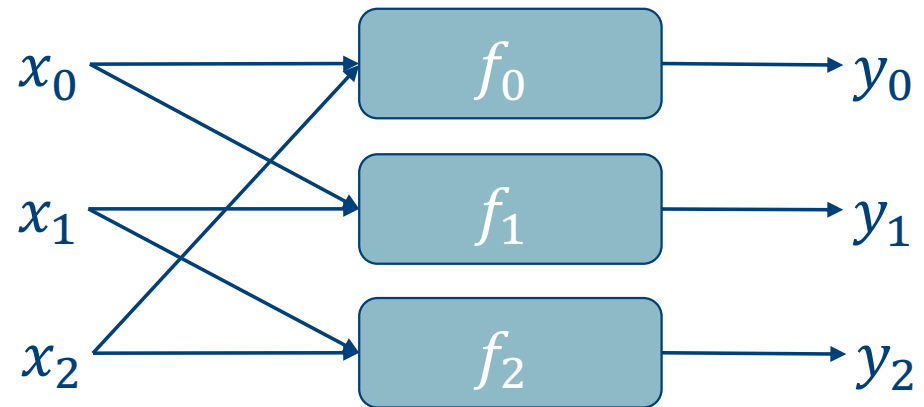
# THRESHOLD IMPLEMENTATIONS





# THRESHOLD IMPLEMENTATIONS [NRS11]

- Non-Completeness

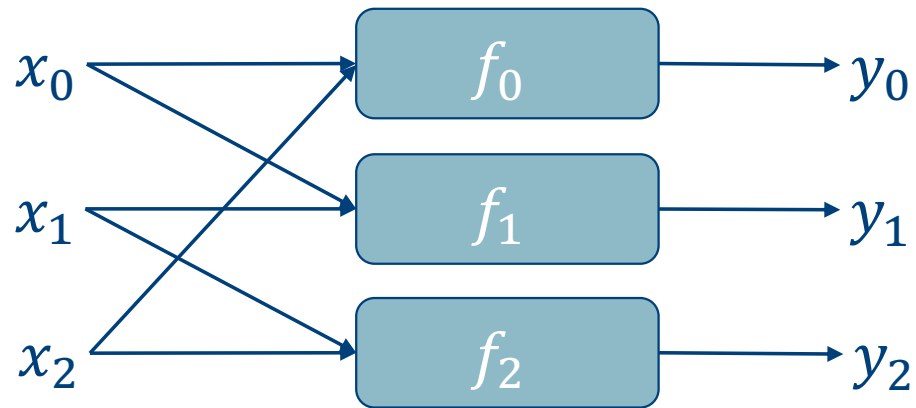


- Uniformity

$$\forall (x_0, x_1, x_2) \text{ s.t. } x_0 \oplus x_1 \oplus x_2 = x:$$
$$\Pr[(x_0, x_1, x_2) | x] = p$$

# THRESHOLD IMPLEMENTATIONS [NRS11]

- Non-Completeness



- Uniformity

$$\forall (x_0, x_1, x_2) \text{ s.t. } x_0 \oplus x_1 \oplus x_2 = x: \\ \Pr[(x_0, x_1, x_2) | x] = p$$


















1-Glitch Extended Probing Security

$$I(\mathcal{R}; x) = 0$$

(Not sufficient for higher-order probing security [RBN+15])

# THRESHOLD IMPLEMENTATIONS [NRS11]

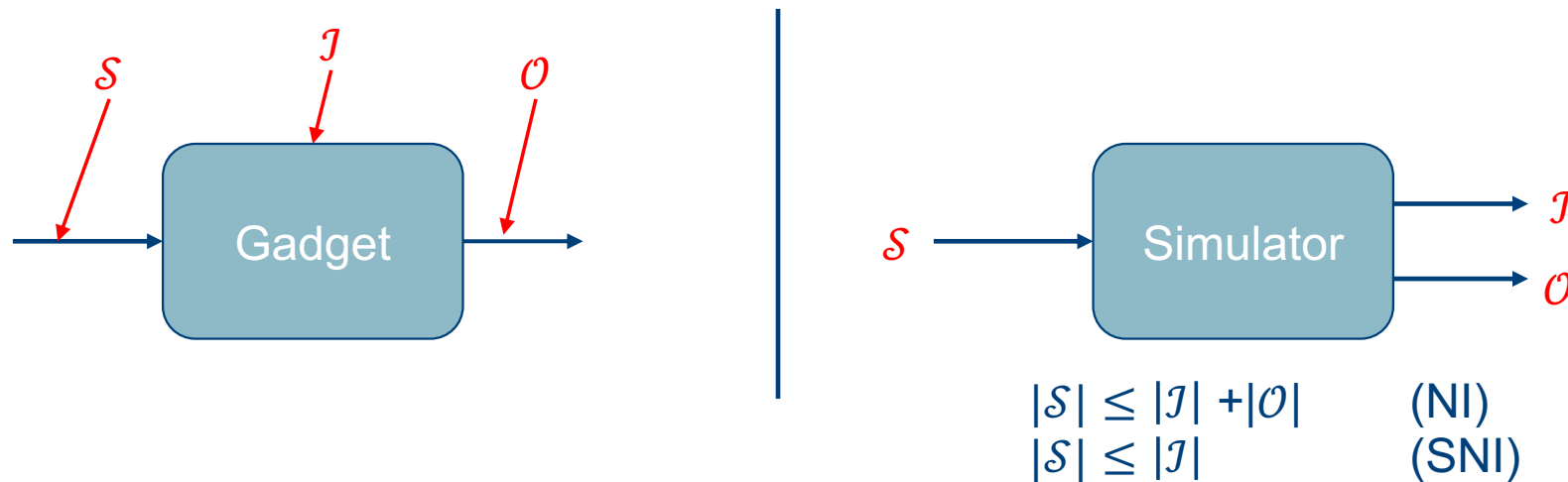
	Non-Completeness	Uniformity	$I(\mathcal{R}; x) = 0$
Sufficient			
Necessary			
Efficient Verification	 [ANR18]		
Multi-variate			
Knowledge required			



(STRONG) NON-INTERFERENCE

# (STRONG) NON-INTERFERENCE [BBD+16]

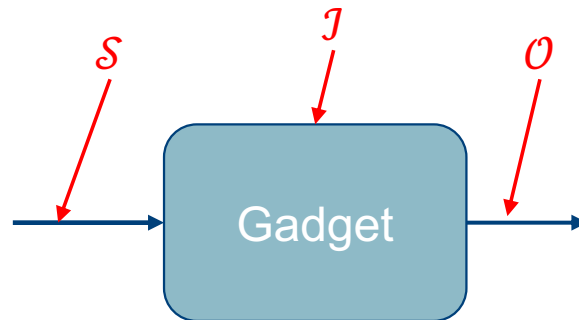
- Notions introduced for composable security
- More efficient verification (MaskVerif [BBF+18])
- Based on simulatability:



- Implies t-probing security

# (STRONG) NON-INTERFERENCE [BBD+16]

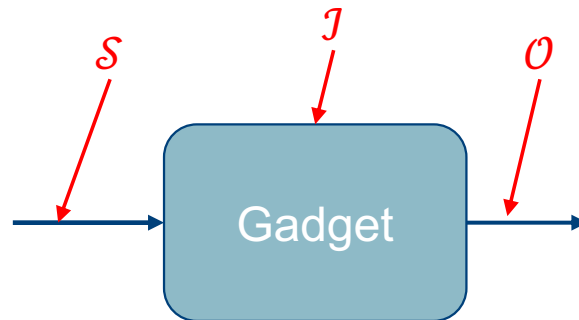
- Originally without glitches
- Extended by robust probing model [FGD+18]
- Unify with mutual information framework:





# (STRONG) NON-INTERFERENCE [BBD+16]

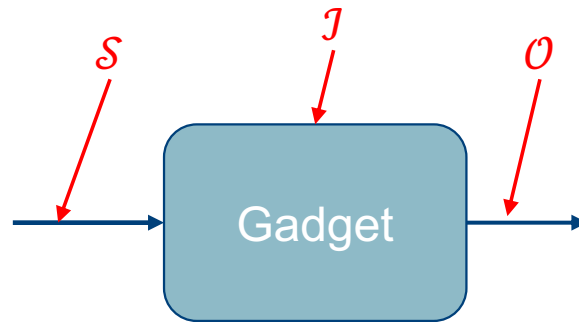
- Originally without glitches
- Extended by robust probing model [FGD+18]
- Unify with mutual information framework:



$$I((\mathcal{J}, \mathcal{O}); \mathbf{x}_{\bar{\mathcal{S}}} | \mathbf{x}_{\mathcal{S}}) = 0$$

# (STRONG) NON-INTERFERENCE [BBD+16]

- Originally without glitches
- Extended by robust probing model [FGD+18]
- Unify with mutual information framework:

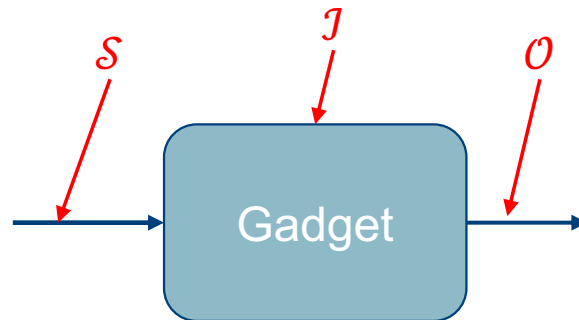


$$I((\mathcal{J}, \mathcal{O}); \mathbf{x}_{\bar{\mathcal{S}}} | \mathbf{x}_{\mathcal{S}}) = 0$$

- Example: output probes & SNI:  $|\mathcal{S}| = 0 \Rightarrow I(\mathcal{O}; \mathbf{x}) = 0$

# (STRONG) NON-INTERFERENCE [BBD+16]

- Originally without glitches
- Extended by robust probing model [FGD+18]
- Unify with mutual information framework:



$$I((\mathcal{J}, \mathcal{O}); \mathbf{x}_{\bar{\mathcal{S}}} | \mathbf{x}_{\mathcal{S}}) = 0$$

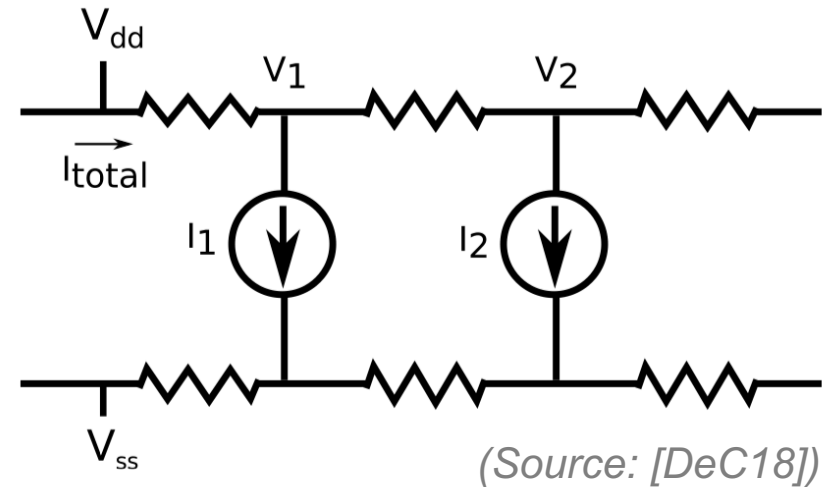
- Example: output probes & SNI:  $|\mathcal{S}| = 0 \Rightarrow I(\mathcal{O}; \mathbf{x}) = 0$
- Glitches?  $\rightarrow$  replace probes with glitch-extended probes

# EXTENDING THE MODELS



# BEYOND GLITCHES

- Gap between theory and practice
  - Coupling [DEM18]
  - CPU leaks [PV17]
  - ...
- Robust Probing Model [FGD+18]
- In the same framework:  $I(\cdot; \cdot) = 0$ 
  - New probe definitions: X-extended probes
  - Same tools!!



# ADVANTAGES

$$I(\cdot; \cdot) = 0$$

- Simple
  - No difference uni-variate or multi-variate
  - No knowledge required on variables
- Any type of masking (Boolean, multiplicative, arithmetic, ...)
- Non-uniformity possible (low entropy masking)
- Versatile
  - Probing/NI/SNI
  - Different models (X-extended probes)
  - Information-theoretic vs practical security (noiseless TVLA)
  - Leakage functions (identity, Hamming, ...)

# CONCLUSION

## consolidate **verb**

con·sol·i·date | \ kən-'sä-lə-,dāt  \

**consolidated; consolidating**

### **Definition of *consolidate***

*transitive verb*

- 1** : to join together into one whole : UNITE  
*// consolidate* several small school districts
- 2** : to make firm or secure : STRENGTHEN  
*// consolidate* their hold on first place  
*// He consolidated* his position as head of the political party.



Thank You