



# Multi-Tuple Leakage Detection and the Dependent Signal Issue

Olivier Bronchain

Tobias Schneider

François-Xavier Standaert

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# Table of Contents

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Introduction

Leakage Detection

Multi-Tuple Leakage Detection

Conclusion

# Content

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Introduction

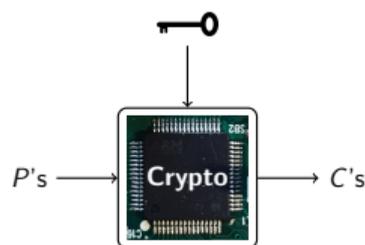
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# Side-Channel Issue

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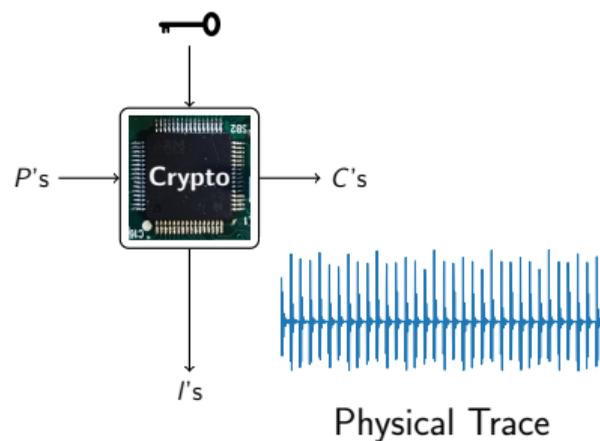


Encryption on physical devices:

- ▶ Standard utilization

# Side-Channel Issue

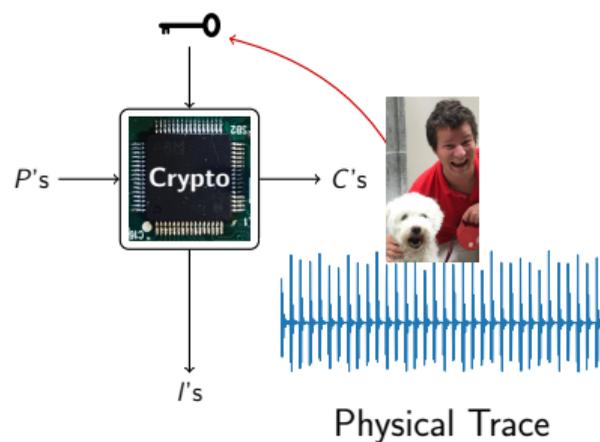
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Encryption on physical devices:

- ▶ Standard utilization
- ▶ But with any physical signals

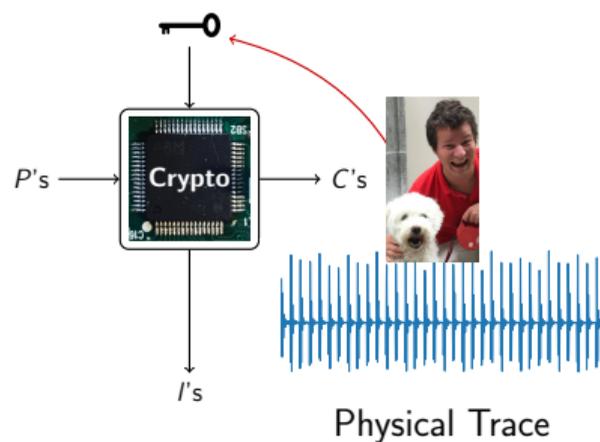
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Encryption on physical devices:

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- ▶ But with any physical signals
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# Side-Channel Issue



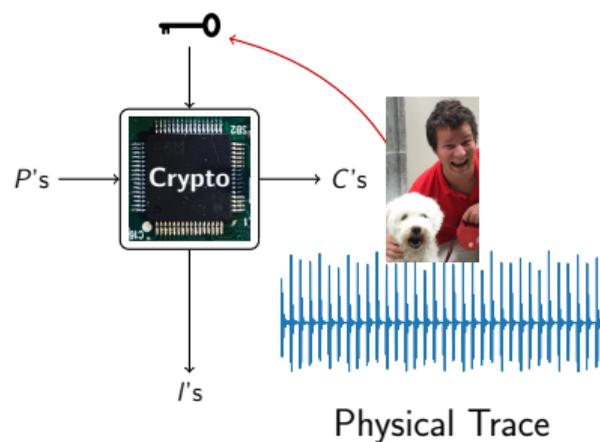
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- ▶ Standard utilization
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Side-channel Attacks:

- ▶ Known to be hard to prevent
- ▶ Hard to evaluate as well

# Side-Channel Issue



Encryption on physical devices:

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- ▶ But with any physical signals
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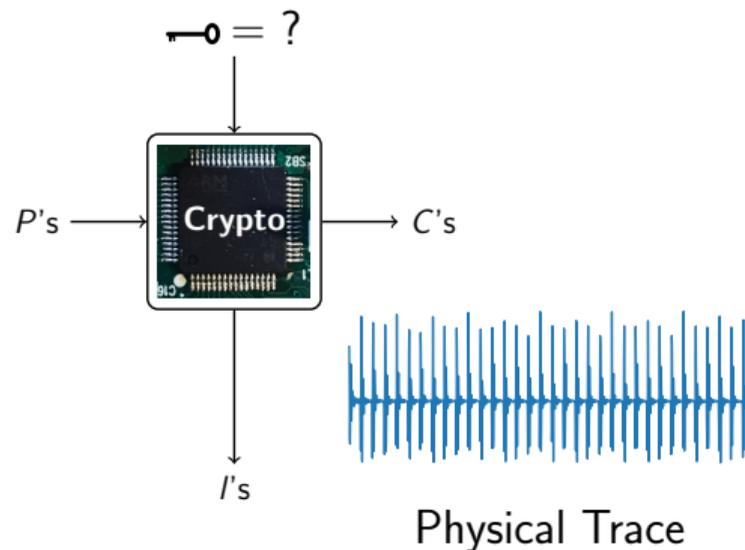
Two evaluation approaches:

- ▶ Attack based
- ▶ Leakage detection

# Attack Based Evaluation

Can directly mount attacks:

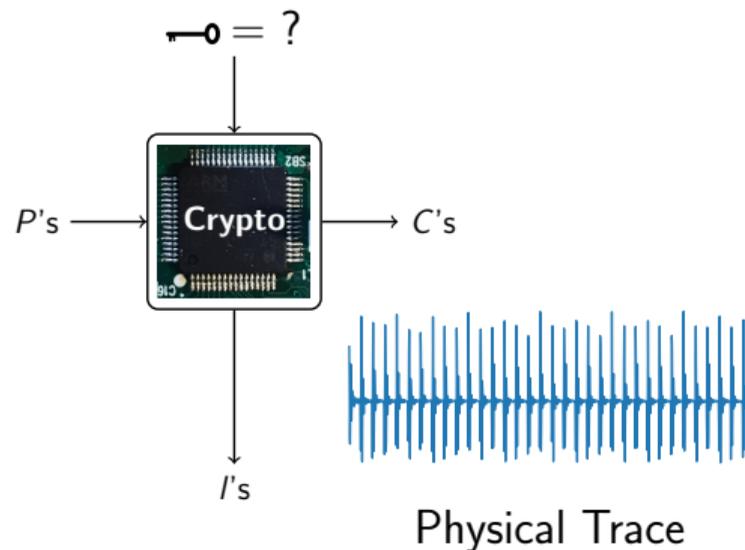
1. Collect measurements



# Attack Based Evaluation

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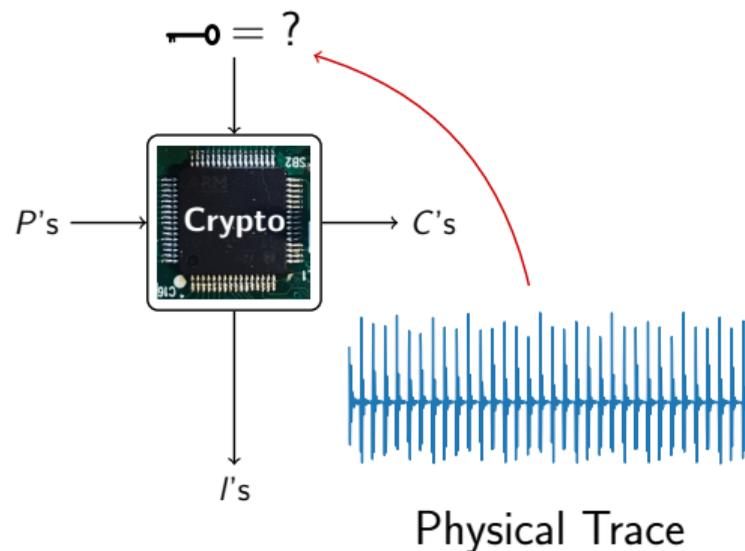
1. Collect measurements
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# Attack Based Evaluation

Can directly mount attacks:

1. Collect measurements
2. Perform an attack
3. Retrieve the correct sub-key



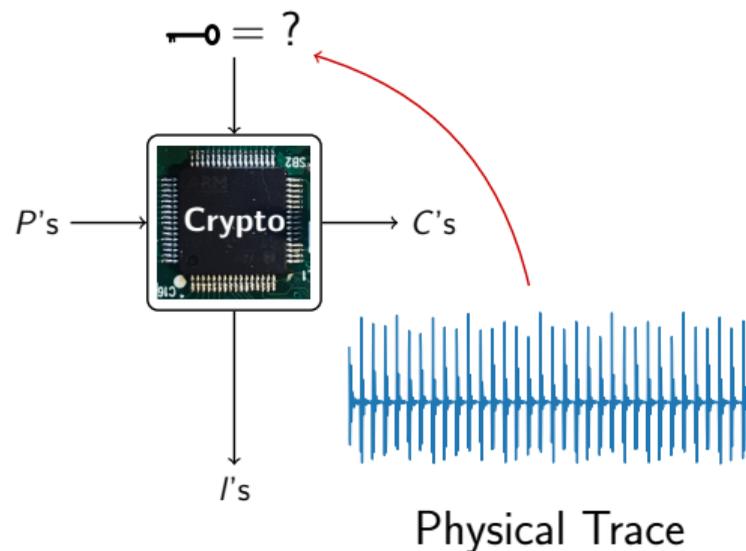
# Attack Based Evaluation

Can directly mount attacks:

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This requires:

1. Long measurement period
2. Skilled/expert knowledge
3. Distinguish 1 sub-key within 256



# Leakage Detection Based Evaluation

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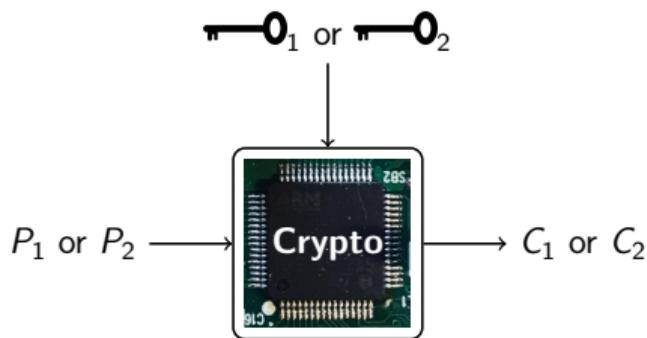
*Leakage detection searches for dependency between manipulated data and physical traces.*



# Leakage Detection Based Evaluation

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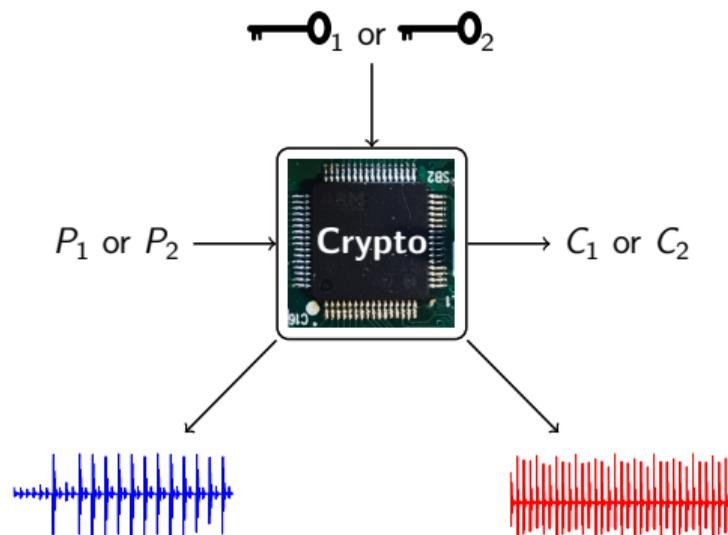
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- Feed the core with two different sets of inputs

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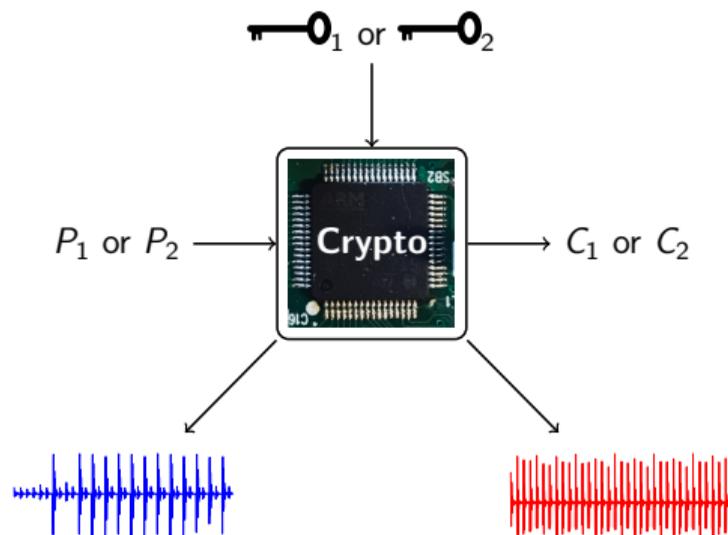
*Leakage detection searches for dependency between manipulated data and physical traces.*



- ▶ Feed the core with two different sets of inputs
- ▶ Record the corresponding traces

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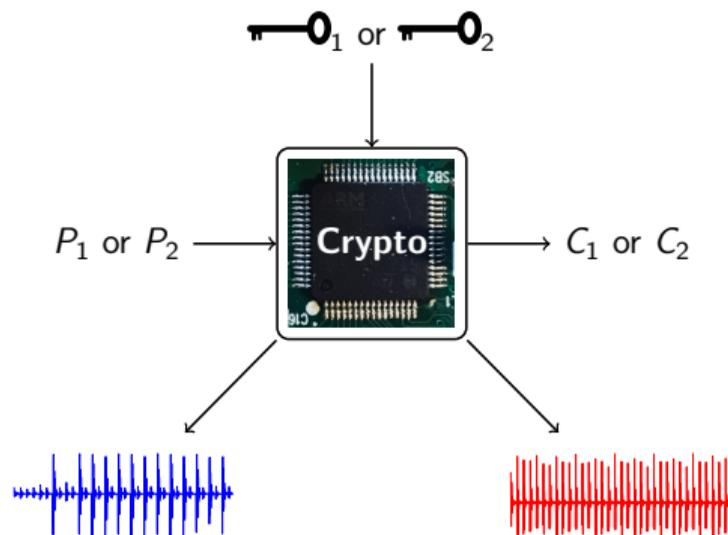
*Leakage detection searches for dependency between manipulated data and physical traces.*



- ▶ Feed the core with two different sets of inputs
- ▶ Record the corresponding traces
- ▶ Observe differences between the two sets

# Leakage Detection Based Evaluation

*Leakage detection searches for dependency between manipulated data and physical traces.*

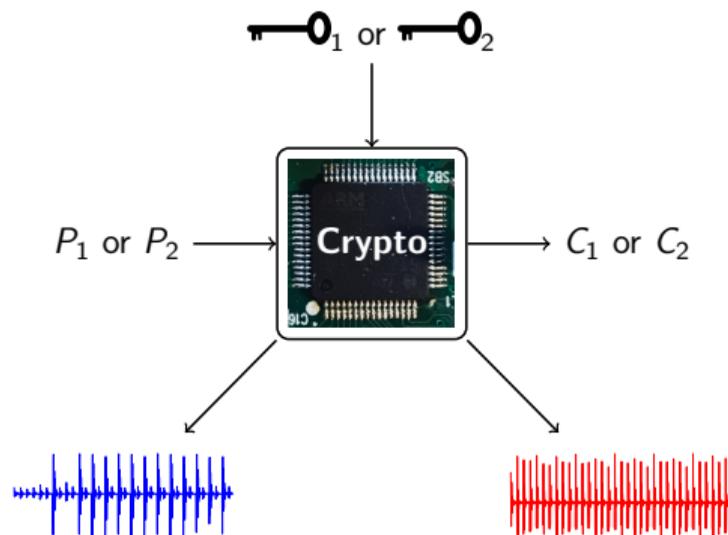


How does it compare with attack based evaluations:

- ▶ Shortened measurement period (Possibly)
- ▶ No skilled/expert knowledge

# Leakage Detection Based Evaluation

*Leakage detection searches for dependency between manipulated data and physical traces.*



How does it compare with attack based evaluations:

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- ▶ No skilled/expert knowledge

A good first check but:

- ▶ Risk of false positives and false negatives

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# Leakage Detection

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Find a difference between the two sets:

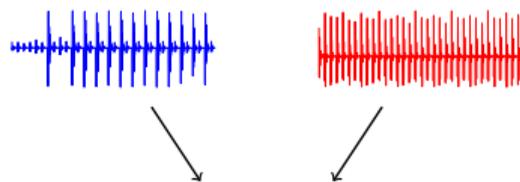


# Leakage Detection

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Find a difference between the two sets:

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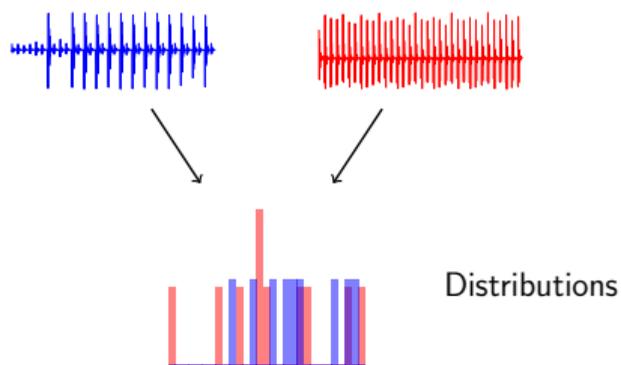


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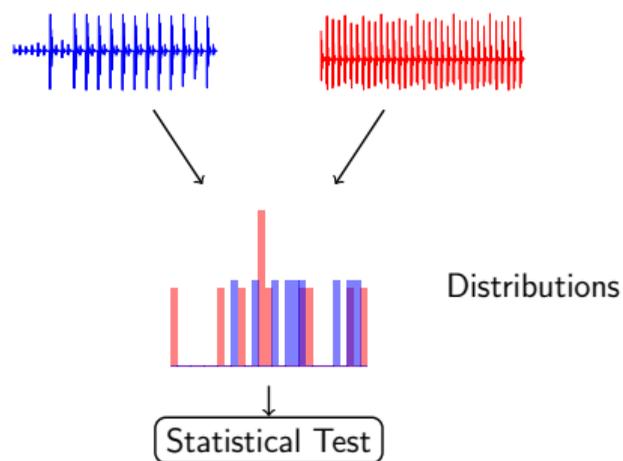
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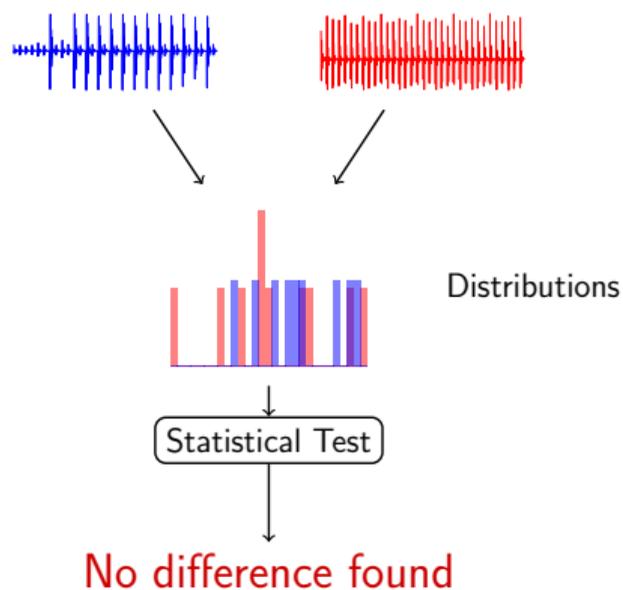
1. Select a point in time
2. Record traces to observe a distribution
3. Perform a statistical test



# Leakage Detection

Find a difference between the two sets:

1. Select a point in time
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3. Perform a statistical test
4. Observe its binary output

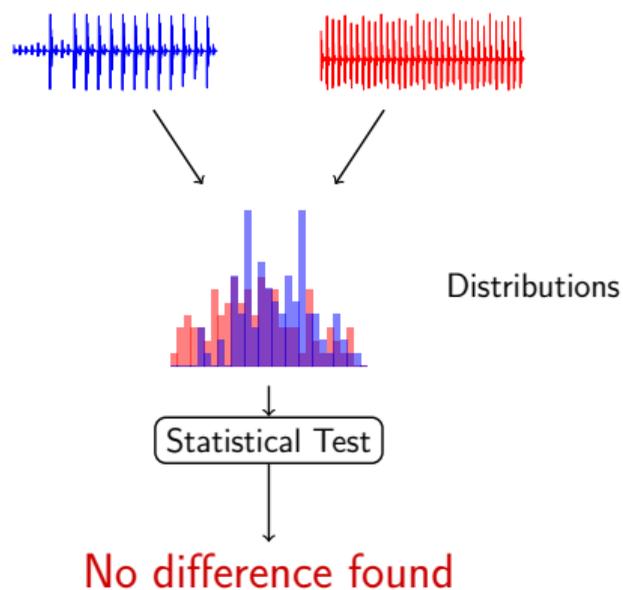


# Leakage Detection

Find a difference between the two sets:

1. Select a point in time
2. Record traces to observe a distribution
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4. Observe its binary output

Repeat with more measurements if needed

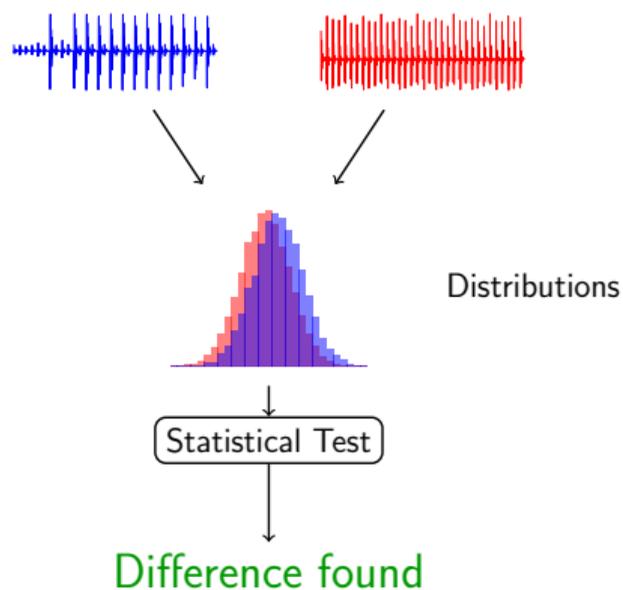


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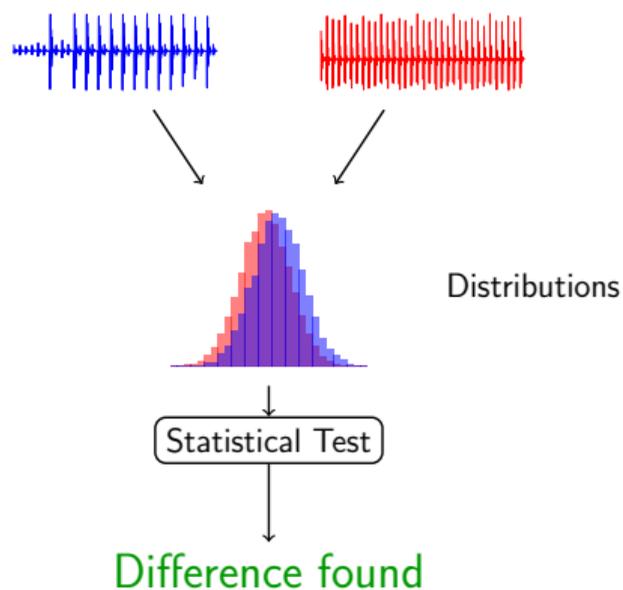
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The statistical test can search for difference in:

- ▶ Means with the Welch's  $t$ -test
- ▶ Distributions with  $\chi^2$ -test
- ▶ ...



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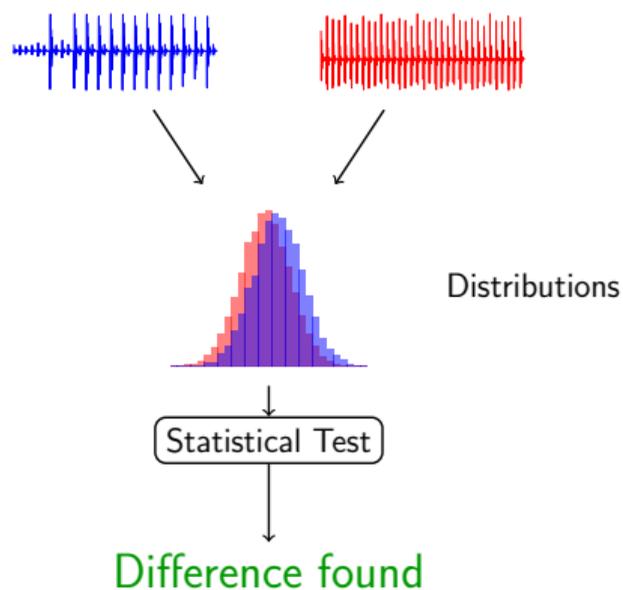
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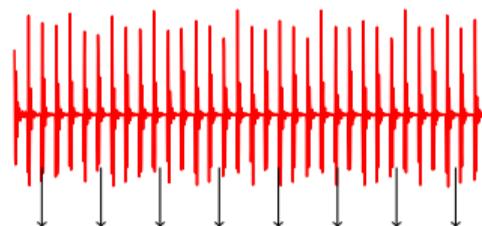


# Leakage Detection: TVLA

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The traces contain multiple points in time:

1. Select **all** the points in time

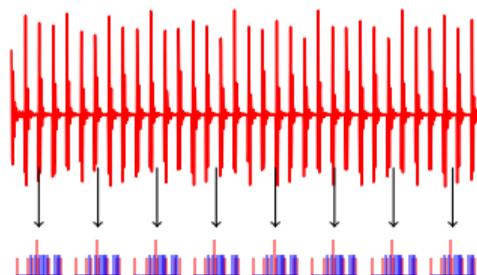


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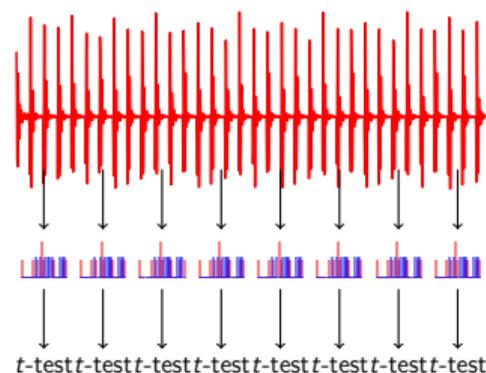


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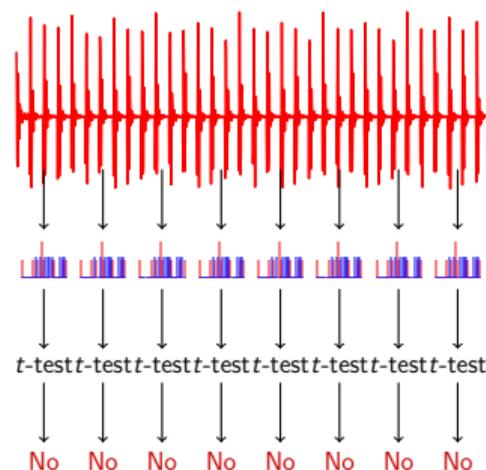
1. Select **all** the points in time
2. Record traces to observe a distribution
3. Perform **independent** statistical test



# Leakage Detection: TVLA

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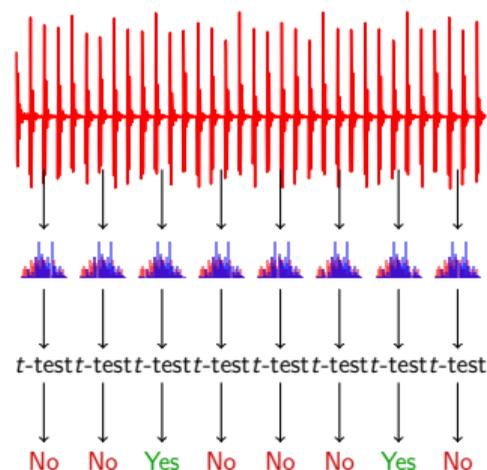
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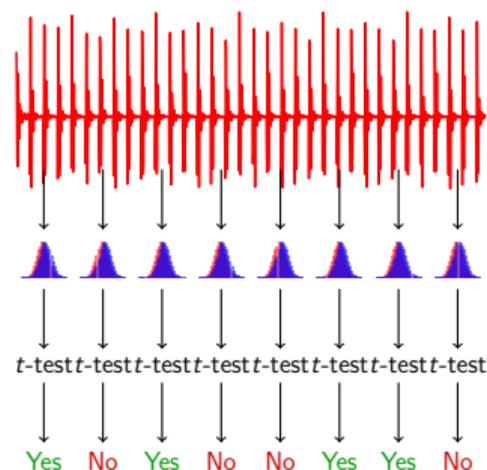
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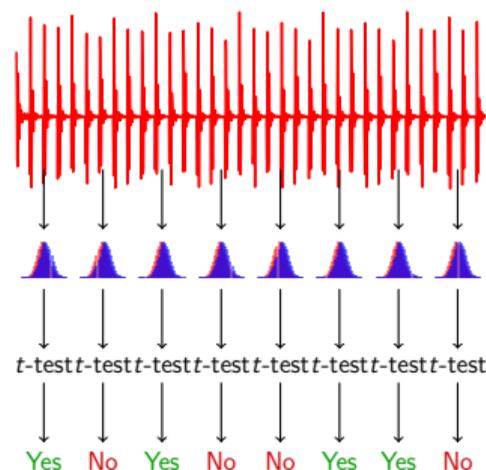
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Difference found if:

- ▶ At least one of the tests goes above a threshold



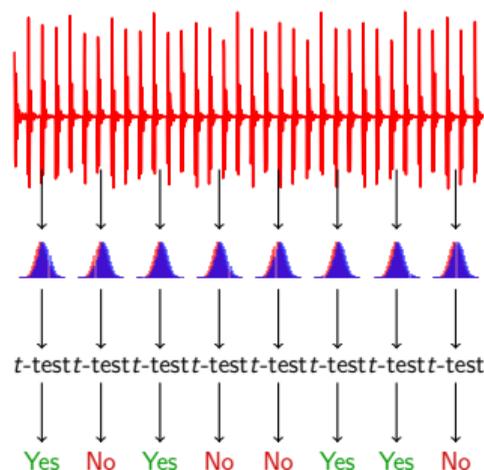
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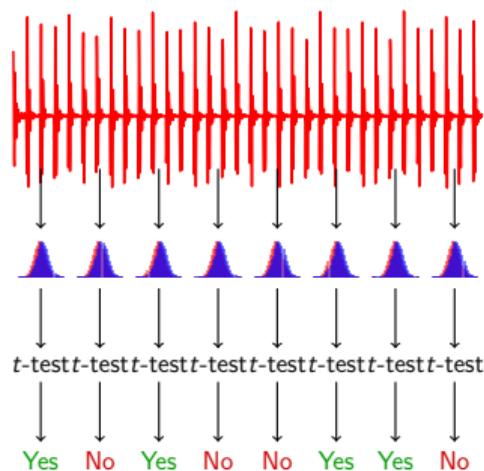
Difference found if:

- ▶ At least one of the tests goes above a threshold
- ▶ Selected thanks to:
  - ▶ Desired confidence
  - ▶ Number of considered time samples
  - ▶ Assuming independence between them



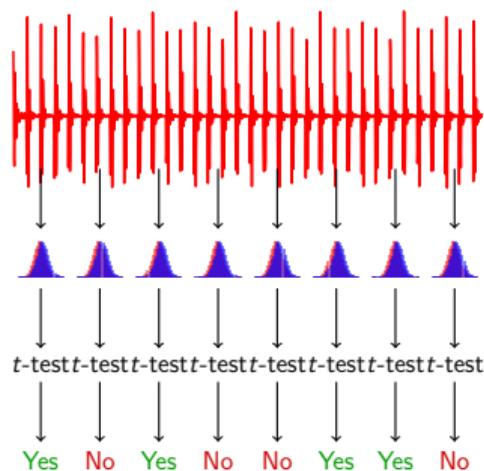
# Limitations to TVLA

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TVLA performs independent  $t$ -test:

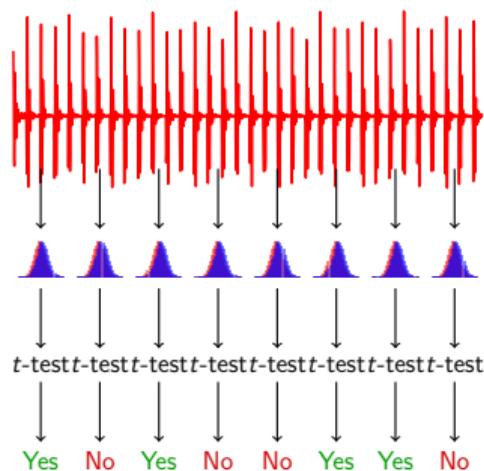
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TVLA performs independent  $t$ -test:

- Impossible to take advantage of multivariate leakage

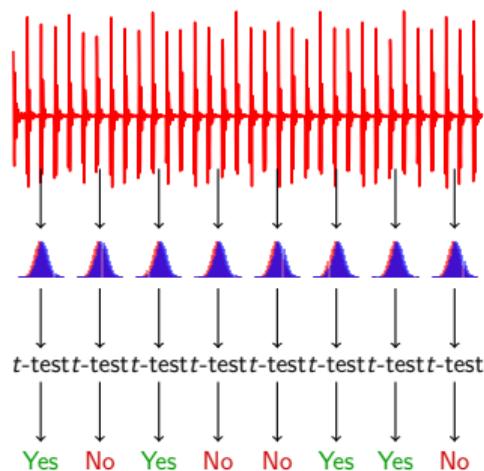
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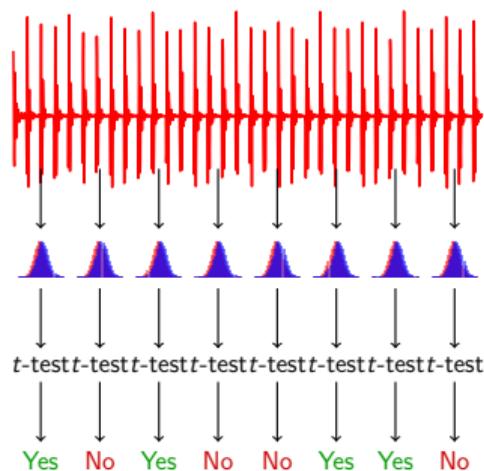


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Independence in the signal is usually not met:

# Limitations to TVLA



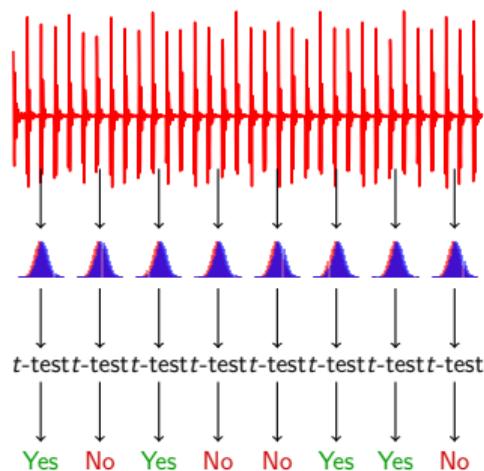
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Independence in the signal is usually not met:

- ▶ Wrong assumption while setting the threshold

# Limitations to TVLA



TVLA performs independent  $t$ -test:

- ▶ Impossible to take advantage of multivariate leakage
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Independence in the signal is usually not met:

- ▶ Wrong assumption while setting the threshold
  - ▶ Hard to interpret results (especially negative ones)

# Content

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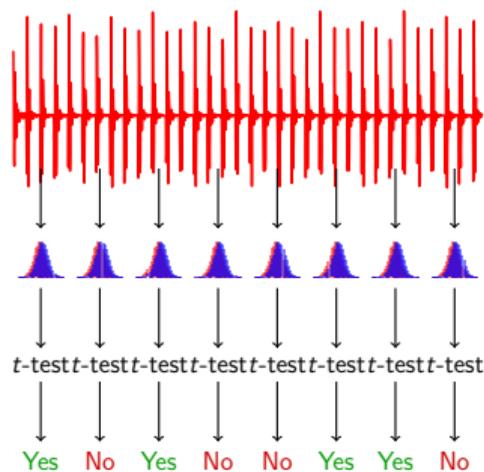
Leakage Detection

**Multi-Tuple Leakage Detection**

Conclusion

# Multi-Tuple Leakage Detection: General Idea

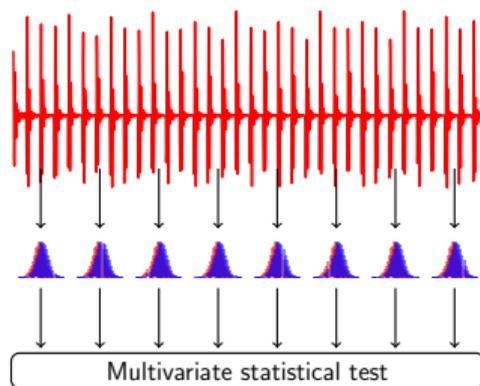
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Approach:

# Multi-Tuple Leakage Detection: General Idea

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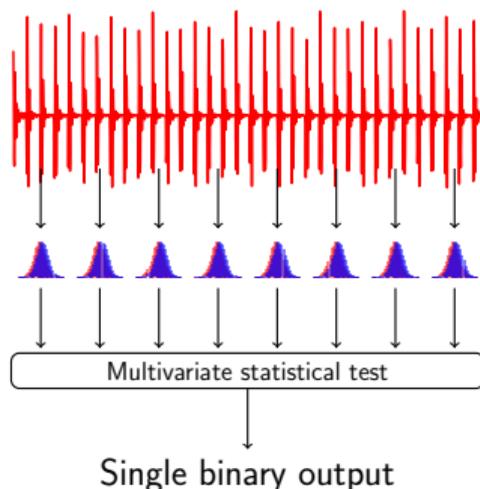


Approach:

- Replace the independent tests by a single one

# Multi-Tuple Leakage Detection: General Idea

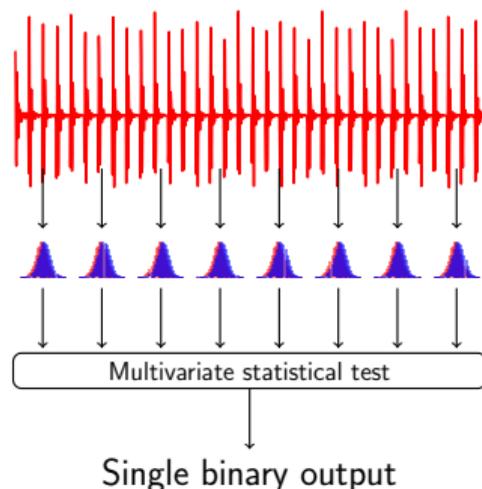
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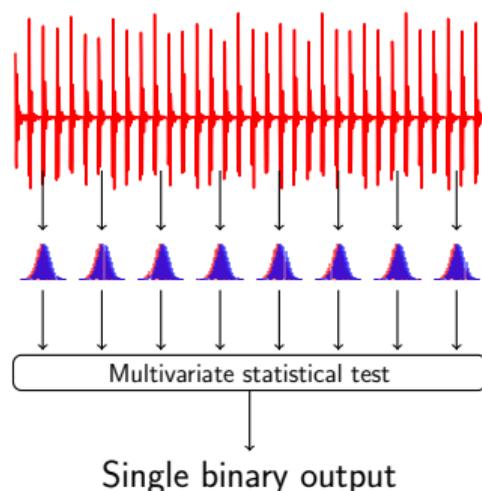
Approach:

- ▶ Replace the independent tests by a single one

**Natural candidate: Hotelling's  $T^2$ -test**

- ▶ Do not assume independence
- ▶ Need to invert a covariance matrix
  - ▶ Not always applicable

# Multi-Tuple Leakage Detection: General Idea



Approach:

- ▶ Replace the independent tests by a single one

**Natural candidate: Hotelling's  $T^2$ -test**

- ▶ Do not assume independence
- ▶ Need to invert a covariance matrix
  - ▶ Not always applicable

**Heuristic alternative:  $D$ -test**

- ▶ Assume independence
  - ▶ Hard to interpret results

# Traces Parameter: Density

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**Density** of informative points:

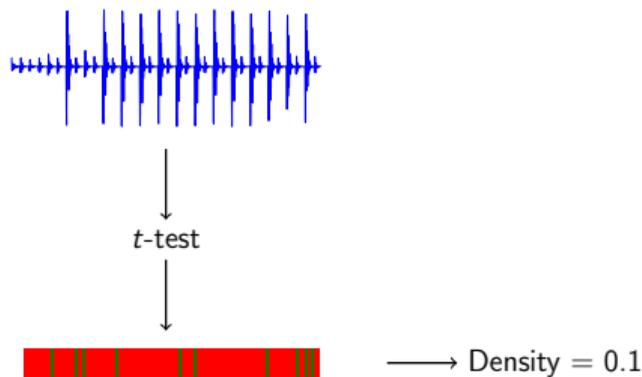
- ▶ The proportion of leaking points
- ▶  $t$ -test showing difference with  $\infty$  of measurements

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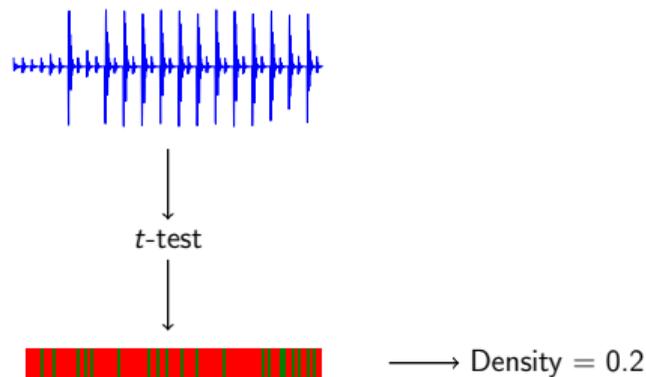


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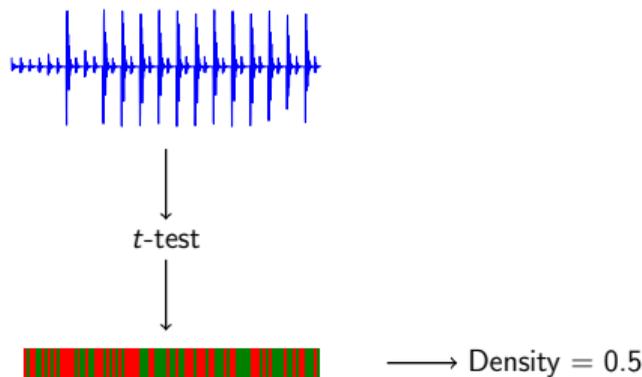


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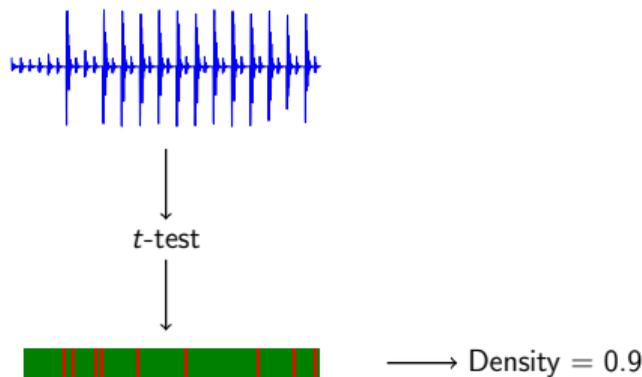


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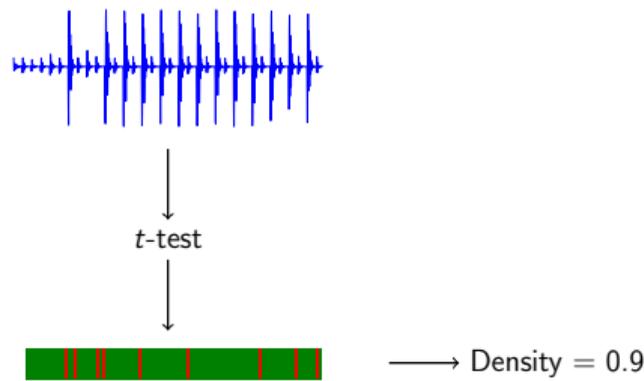


# Traces Parameter: Density

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**Density** of informative points:

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Typical settings:

- ▶ Protected software: low density, long traces
- ▶ Hardware unprotected: high density, short traces

# Multi-Tuple Leakage Detection: Features

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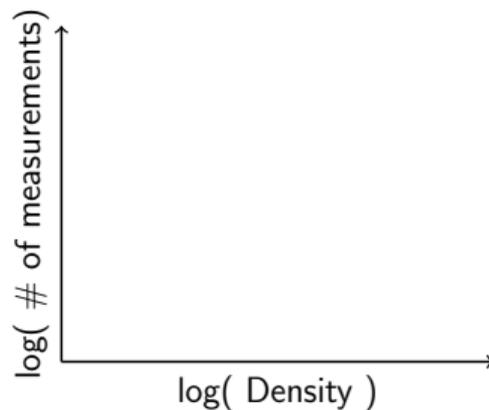
From simulations with fixed trace length:

—————→  
log( Density )

# Multi-Tuple Leakage Detection: Features

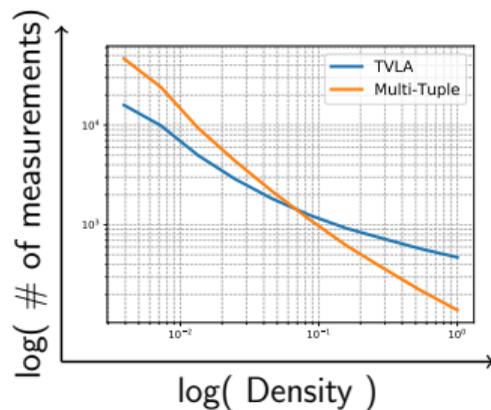
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# Multi-Tuple Leakage Detection: Features

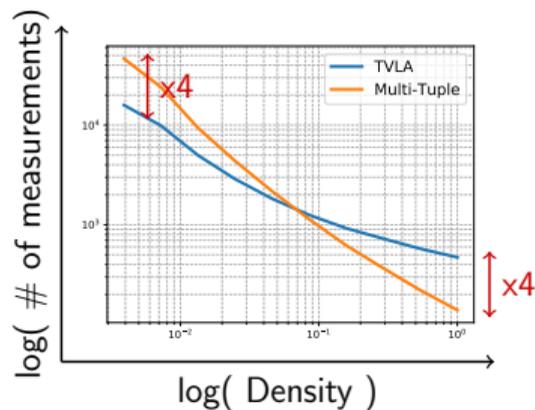
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# Multi-Tuple Leakage Detection: Features

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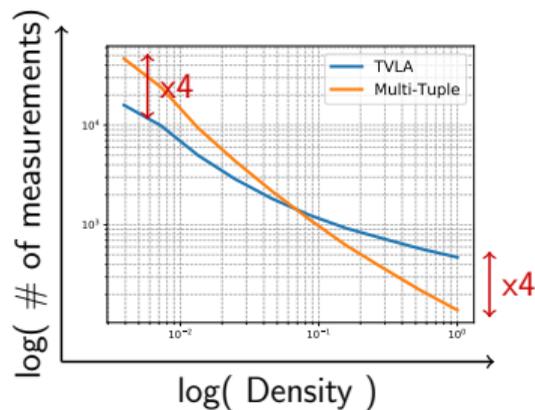
- ▶ Both methods suffer from a low density



# Multi-Tuple Leakage Detection: Features

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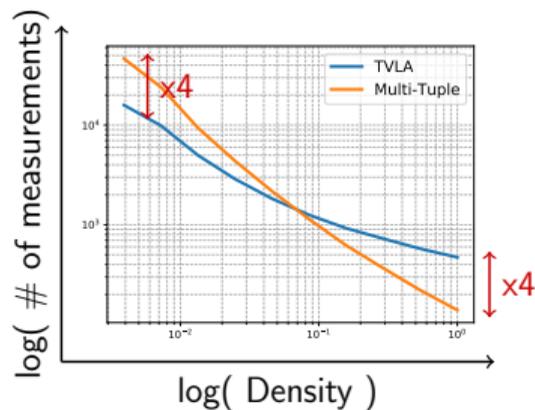
- ▶ Both methods suffer from a low density
- ▶ Multi-Tuple more than the TVLA



# Multi-Tuple Leakage Detection: Features

From simulations with fixed trace length:

- ▶ Both methods suffer from a low density
- ▶ Multi-Tuple more than the TVLA



Reduced data complexity with **higher density**

# Multi-Tuple Leakage Detection: Parameters

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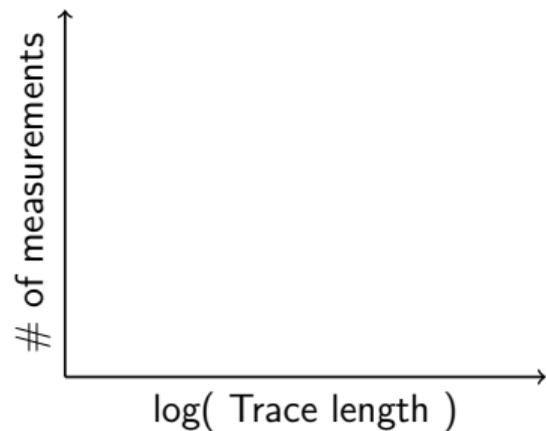
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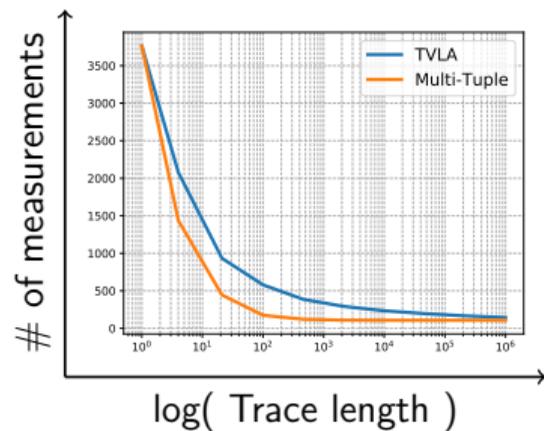
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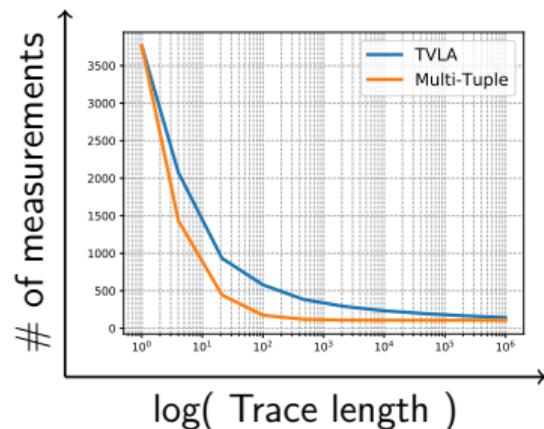
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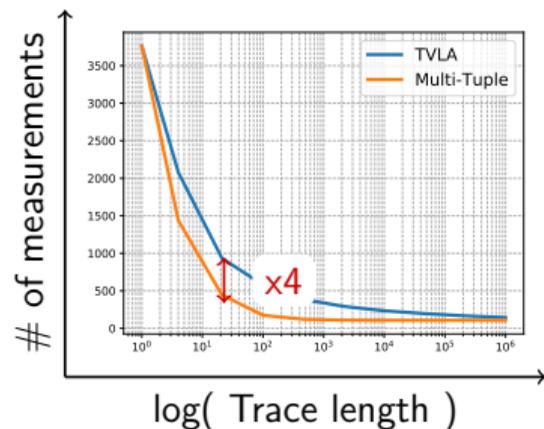
- ▶ Both methods take advantage of longer traces



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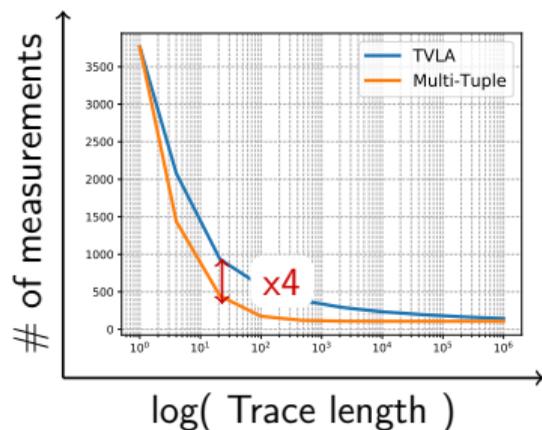
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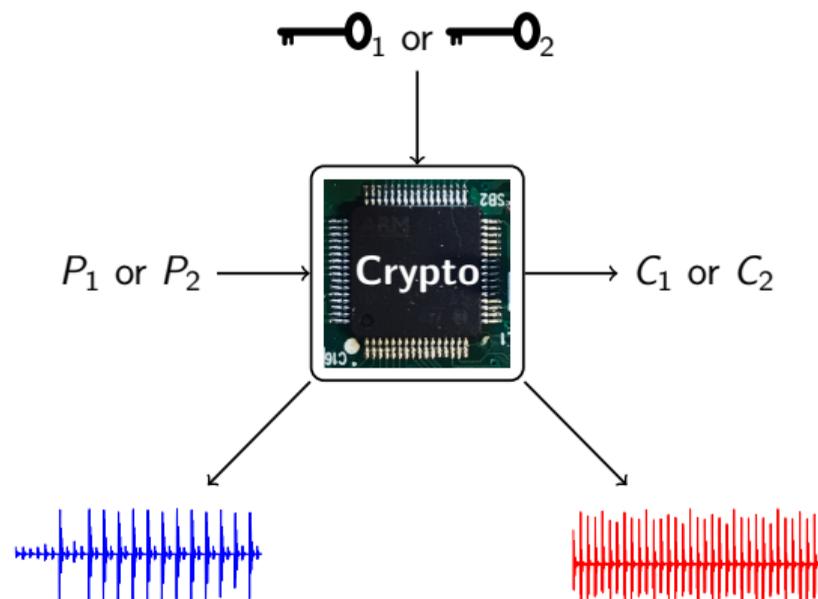
- ▶ Both methods take advantage of longer traces
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- ▶ Reduced data complexity with the **number of time samples**
- ▶ The jointly processed trace size is limited for Hotelling's test because of covariance matrix inversion ( $\sim 2000$ ):
  - ▶ Possibility to run multiple Hotelling's tests in parallel

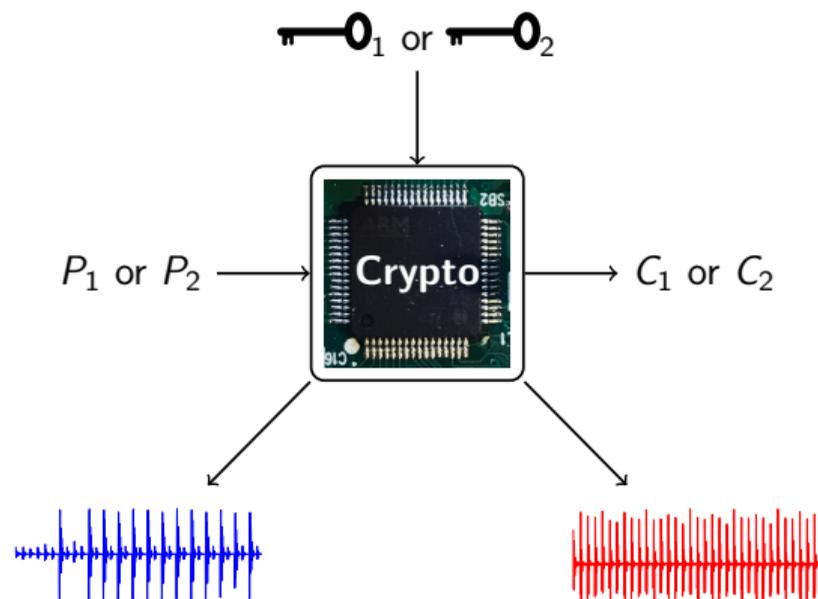
# Practical Evaluation Scenarios

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Two extreme settings:

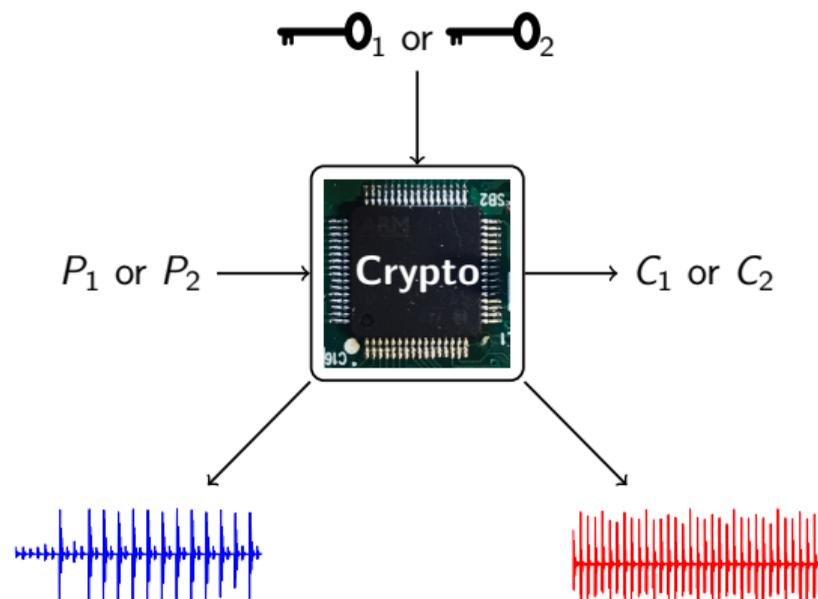
# Practical Evaluation Scenarios



Two extreme settings:

- ▶ White Box: everything is known about the design

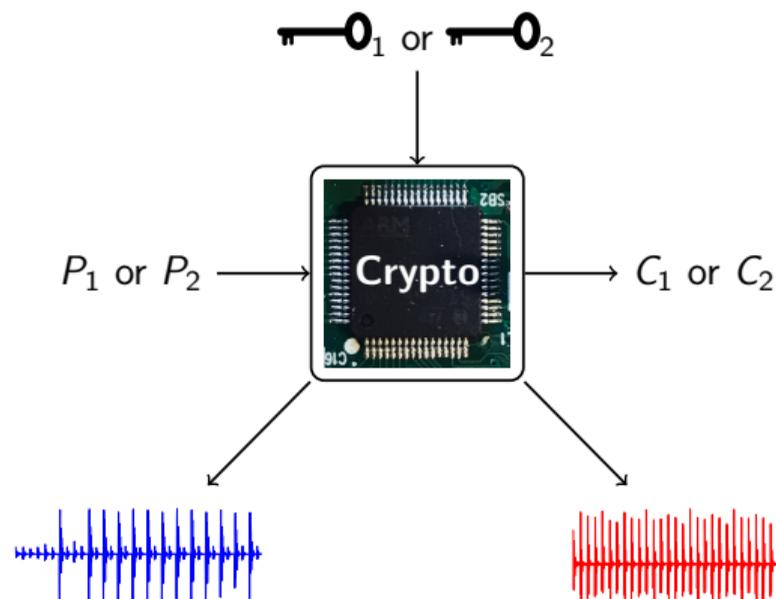
# Practical Evaluation Scenarios



Two extreme settings:

- ▶ White Box: everything is known about the design
- ▶ Black Box: nothing is known about the design

# Practical Evaluation Scenarios



Two extreme settings:

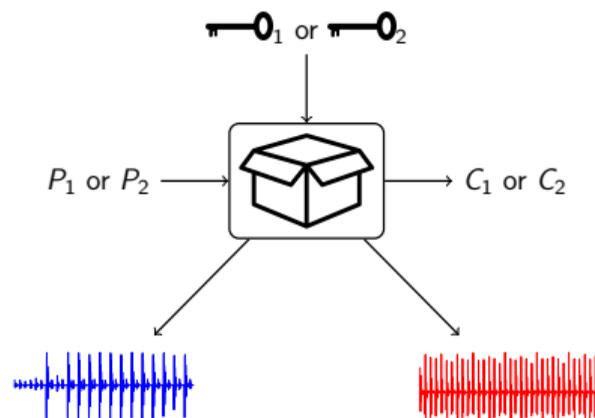
- ▶ White Box: everything is known about the design
- ▶ Black Box: nothing is known about the design

## How to perform Leakage Detection in these settings ?

# Practical Evaluation Scenarios: White Box

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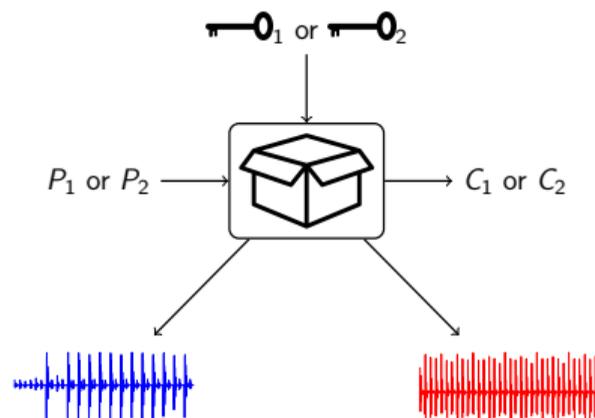
In White Box:



# Practical Evaluation Scenarios: White Box

In White Box:

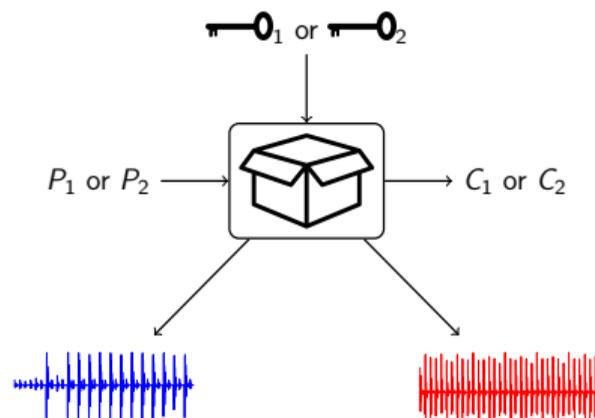
- ▶ Prior information about leaking points



# Practical Evaluation Scenarios: White Box

In White Box:

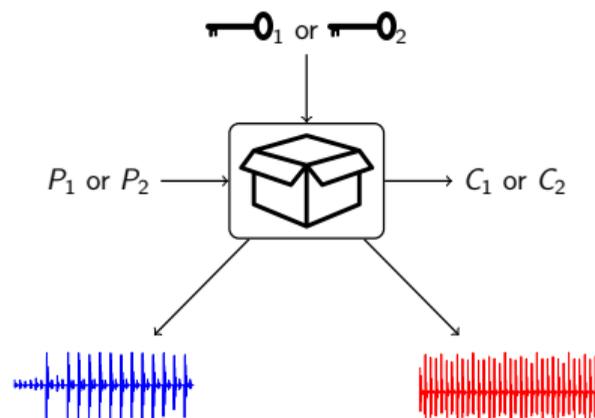
- ▶ Prior information about leaking points
  - ▶ Can reduce traces



# Practical Evaluation Scenarios: White Box

In White Box:

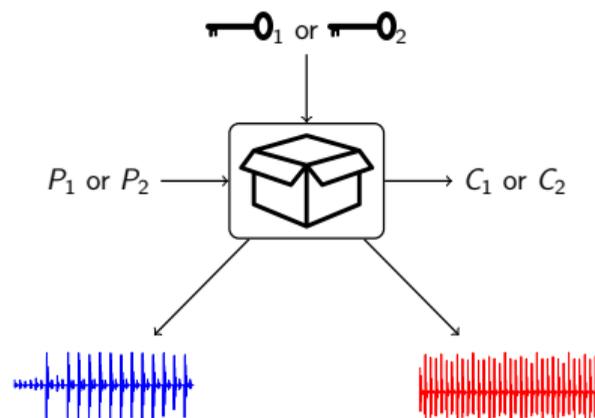
- ▶ Prior information about leaking points
  - ▶ Can reduce traces
    - ▶ Can invert the covariance matrix (Hotelling's  $T^2$ -test)
    - ▶ High density



# Practical Evaluation Scenarios: White Box

In White Box:

- ▶ Prior information about leaking points
  - ▶ Can reduce traces
    - ▶ Can invert the covariance matrix (Hotelling's  $T^2$ -test)
    - ▶ High density

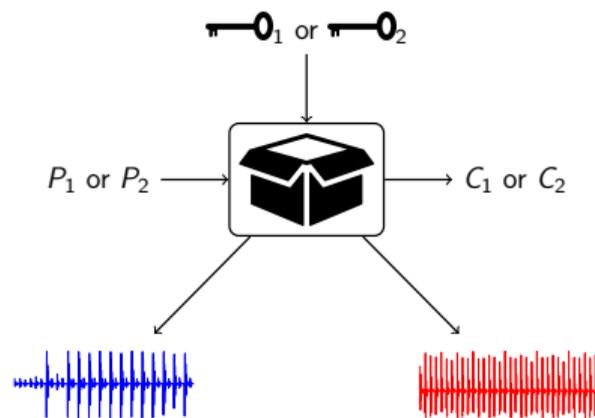


As a result:

- ▶ Smaller measurement period
- ▶ Easy interpretation of the confidence (no  $\perp$  assumption)

# Practical Evaluation Scenarios: Black Box

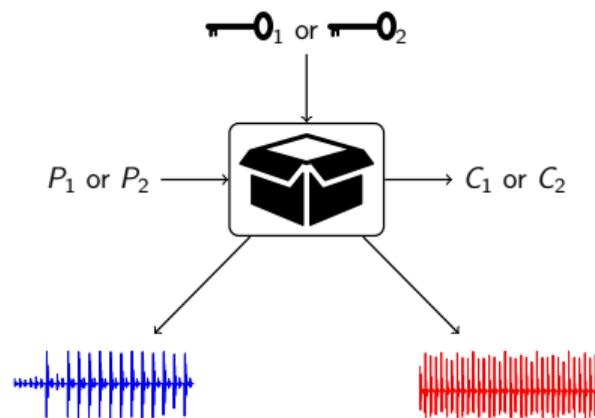
In Black Box:



# Practical Evaluation Scenarios: Black Box

In Black Box:

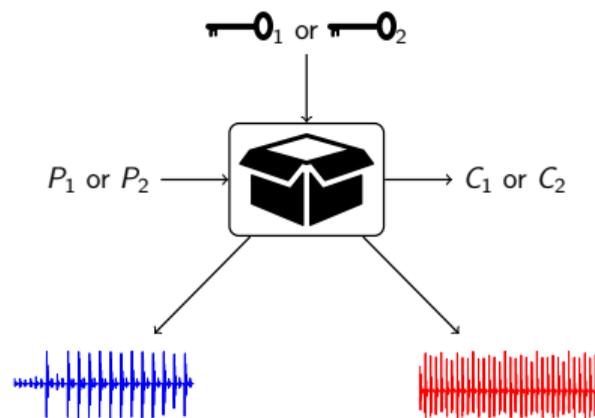
- ▶ No prior information about leaking points



# Practical Evaluation Scenarios: Black Box

In Black Box:

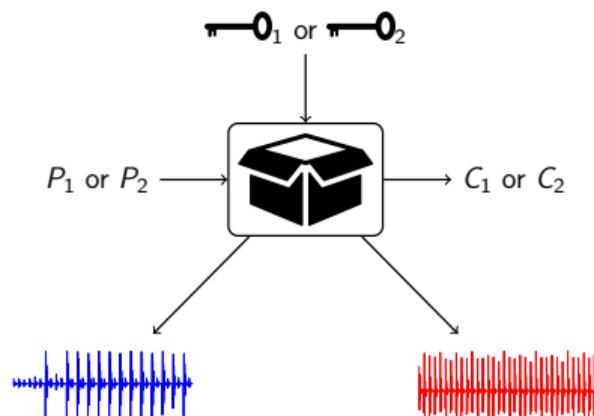
- ▶ No prior information about leaking points
  - ▶ Can't reduce traces



# Practical Evaluation Scenarios: Black Box

In Black Box:

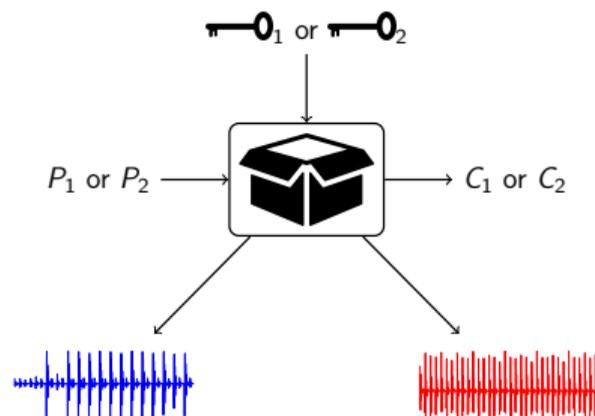
- ▶ No prior information about leaking points
  - ▶ Can't reduce traces
    - ▶ Can't always invert the covariance matrix



# Practical Evaluation Scenarios: Black Box

In Black Box:

- ▶ No prior information about leaking points
  - ▶ Can't reduce traces
    - ▶ Can't always invert the covariance matrix
    - ▶ Fixed density



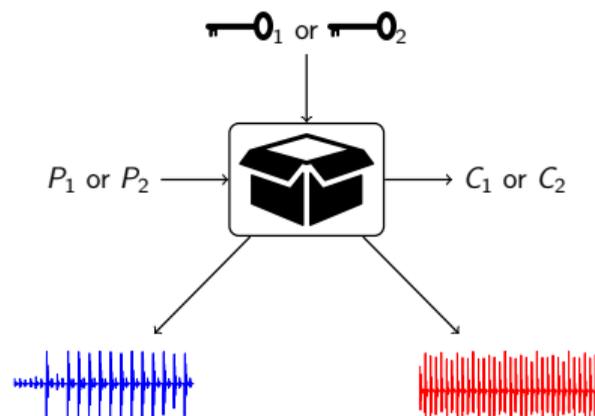
# Practical Evaluation Scenarios: Black Box

In Black Box:

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As a result:

- ▶ Possibly larger measurement period



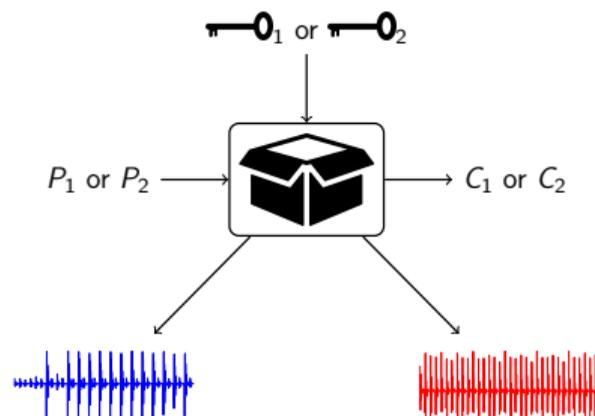
# Practical Evaluation Scenarios: Black Box

In Black Box:

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As a result:

- ▶ Possibly larger measurement period
- ▶ Independent assumption needed



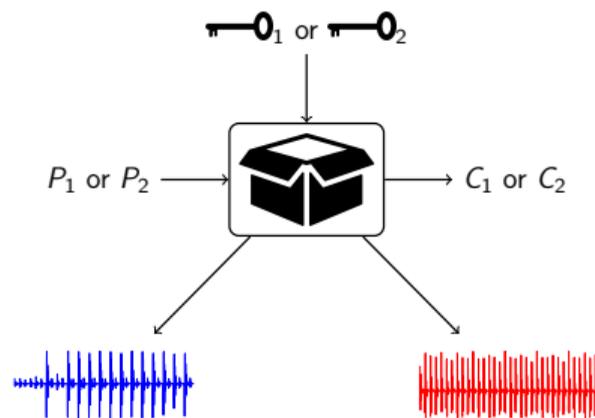
# Practical Evaluation Scenarios: Black Box

In Black Box:

- ▶ No prior information about leaking points
  - ▶ Can't reduce traces
    - ▶ Can't always invert the covariance matrix
    - ▶ Fixed density

As a result:

- ▶ Possibly larger measurement period
- ▶ Independent assumption needed
  - ▶ Heuristic required for confidence level interpretation:
    - ▶ TVLA: too conservative
    - ▶  $D$ -test: too optimistic



# Content

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Introduction

Leakage Detection

Multi-Tuple Leakage Detection

Conclusion

# Conclusion

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Physical signals are not likely to be independent across time

# Conclusion

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Physical signals are not likely to be independent across time

1. If applicable, Hotelling's  $T^2$ -test provides:

# Conclusion

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Physical signals are not likely to be independent across time

1. If applicable, Hotelling's  $T^2$ -test provides:
  - ▶ Straight forward interpretation of the confidence level
  - ▶ And sometimes reduction the measurement period
  - ▶ Loose intuition about the POIs

# Conclusion

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Physical signals are not likely to be independent across time

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2. If not, must rely on heuristics:

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Evaluation Hardness

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Thanks !

A horizontal arrow with a green-to-red gradient pointing to the right, indicating a transition or progression.

Evaluation Hardness

[github.com/obronchain/multiple\\_leakage\\_detection](https://github.com/obronchain/multiple_leakage_detection)