

# Standard Lattice-Based Key Encapsulation on Embedded Devices

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## Outline

- 🔥 Post-quantum cryptography and LWE
- 🔥 Motivation
- 🔥 Introduction to Frodo
- 🔥 Microcontroller design
- 🔥 Hardware design
- 🔥 Results and performance analysis



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## Motivation

- ✦ NIST have started a post-quantum standardisation “competition”.
- ✦ The call suggests future rounds will likely involve:
  - ▶ Evaluations on constrained devices, such as smart cards,
  - ▶ as well as comparisons of the schemes in hardware.
- ✦ Why focus on lattice-based / Frodo?
  - ▶ Extremely versatile and theoretically sound.
  - ▶ Probably the most secure lattice candidate.
  - ▶ Less implementations than ideal lattice schemes; has larger keys and no NTT.
  - ▶ Frodo is ideal for long-term security and constrained (hardware) platforms.



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## Frodo: Take off the ring!

The design philosophy of FrodoKEM [ABD<sup>+</sup>] combines:

- ✦ Conservative yet practical post-quantum constructions.
- ✦ Security derived from cautious parameterizations of the well-studied learning with errors problem.
- ✦ Thus, close connections to conjectured-hard problems on generic, “algebraically unstructured” lattices.
- ✦ Parameter selection is far less constrained than vs ideal lattice schemes.

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## Frodo: Why should we take off the ring?

These qualities are appealing for practitioners;

- ✦ Many IoT use cases require long-term, efficient cryptography.
- ✦ Post-quantum cryptography is becoming essential.
- ✦ Microcontrollers and FPGAs will play a role in future technologies.
- ✦ Suitable for use cases such as satellite communications and V2X.

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## Frodo: key encapsulation from standard lattices

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### Algorithm 1 The FrodoKEM encapsulation (shortened)

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- 1: **procedure** ENCAPS( $pk = \text{seed}_A || \mathbf{b}$ )
  - 2:   Choose a uniformly random key  $\mu \leftarrow U(\{0, 1\}^{\text{len}_\mu})$
  - 3:   Generate pseudo-random values  $\text{seed}_E || \mathbf{k} || \mathbf{d} \leftarrow G(pk || \mu)$
  - 4:   Sample error matrix  $\mathbf{S}', \mathbf{E}' \leftarrow \text{Frodo.SampleMatrix}(\text{seed}_E, \bar{m}, n, T_\chi, \cdot)$
  - 5:   Generate the matrix  $\mathbf{A} \in \mathbb{Z}_q^{n \times n}$  via  $\mathbf{A} \leftarrow \text{Frodo.Gen}(\text{seed}_A)$
  - 6:   Compute  $\mathbf{C}_1 \leftarrow \mathbf{S}' \mathbf{A} + \mathbf{E}'$
  - 7:   Sample error matrix  $\mathbf{E}'' \leftarrow \text{Frodo.SampleMatrix}(\text{seed}_E, \bar{m}, \bar{n}, T_\chi, \cdot)$
  - 8:   Compute  $\mathbf{C}_2 \leftarrow \mathbf{S}' \mathbf{B} + \mathbf{E}'' + \text{Frodo.Encode}(\mu)$
  - 9:   Compute  $ss \leftarrow F(\mathbf{c}_1 || \mathbf{c}_2 || \mathbf{k} || \mathbf{d})$
  - 10:   **return** ciphertext  $\mathbf{c}_1 || \mathbf{c}_2 || \mathbf{d}$  and shared secret  $ss$
  - 11: **end procedure**
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## Frodo: key encapsulation from standard lattices

FrodoKEM is comprised of a number of key modules:

- ✦ Matrix-matrix multiplication, up to sizes 976.
- ✦ Uniform and “Gaussian” error generation.
- ✦ Random oracles via cSHAKE for CCA security.

A massive design challenge was to balance **memory utilisation**, whilst not deteriorating the **performance** too much to not overexert the limited computing capabilities of the embedded devices.

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## FrodoKEM on constrained devices

FrodoKEM has a number of design options we cover:

- ✦ Both sets of parameters;
  - ▶ FrodoKEM-640 aims to match AES-128 security.
  - ▶ FrodoKEM-976 aims to match AES-192 security.
- ✦ PRNG from AES and cSHAKE modules.
- ✦ We focus on FrodoKEM, rather than the previous key exchange scheme FrodoCCS [BCD<sup>+</sup>16].



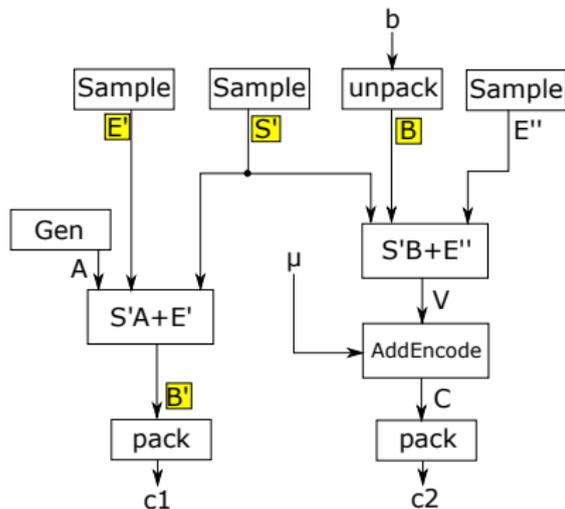
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## FrodoKEM on ARM

### Contribution overview:

- ✦ Optimized memory allocation that makes the implementation small enough to fit on embedded microcontrollers.
- ✦ An assembly multiplication routine that speeds up our implementation, realizing a performance that fits the requirements of common use-cases.
- ✦ Utilises constant runtime to protect against simple side-channel analysis.
- ✦ FrodoKEM-640 has a total execution time of 836 ms, running at 168 MHz.

## FrodoKEM on ARM



- ✦ We analysed the memory occupancy during each operation.
- ✦ Wherever possible, reusing already allocated memory.
- ✦ This minimised the memory usage for all designs.
- ✦ Memory usage for AES versions much simpler than for cSHAKE versions.

Figure: FrodoKEM encaps flowchart.

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## Results and Comparisons

- ✂ Clear difference between AES and cSHAKE implementations.
- ✂ Due to more efficient AES [SS16], cSHAKE needs load/save from RAM.
- ✂ Outperforms other Frodo design, but much slower than Kyber / NewHope.

**Table:** Cycle counts for our full microcontroller implementations (at 168 MHz).

Implementation	Platform	Security Level	Cycle counts
FrodoKEM-640-AES	Cortex-M4	128 bits	140,398,055
FrodoKEM-976-AES	Cortex-M4	192 bits	315,600,317
FrodoKEM-640-cSHAKE	Cortex-M4	128 bits	310,131,435
FrodoKEM-976-cSHAKE	Cortex-M4	192 bits	695,001,098
FrodoKEM-640-cSHAKE [pqm]	Cortex-M4	128 bits	318,037,129
KyberNIST-768 [pqm]	Cortex-M4	192 bits	4,224,704
NewHopeUSENIX-1024 [AJS16]	Cortex-M4	255 bits	2,561,438
ECDH scalar multiplication [DHH <sup>+</sup> 15]	Cortex-M0	pre-quantum	3,589,850

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## Results and Comparisons

- ✦ Despite being slower, cSHAKE requires less memory than AES.
- ✦ Our memory optimisations save between 30-40% compared to PQM4.
- ✦ Versus the referenced designs we also save 66% in peak stack usage.

**Table:** Stack usage in bytes for our microcontroller implementations.

Operation	FrodoKEM-AES		FrodoKEM-cSHAKE		FrodoKEM-cSHAKE [pqm]	
	$n = 640$	$n = 976$	$n = 640$	$n = 976$	$n = 640$	% Savings
Keypair	23,396	35,484	22,376	33,800	36,536	39%
Encaps	41,292	63,484	37,792	57,968	58,328	35%
Decaps	51,684	63,628	48,184	58,112	68,680	30%

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## FrodoKEM on FPGA

### Contribution overview:

- ✦ Proposes a generic LWE multiplication core which computes vector-matrix multiplication and error addition.
- ✦ Generates future random values in parallel, minimising delays between vector-matrix multiplications.
- ✦ Hybrid pre-calculated / on-the-fly memory management is used, which continuously updates previous values.
- ✦ Ensures constant runtime by parallelising other modules with multiplication.
- ✦ FrodoKEM-640 has a total execution time of 60 ms, running at 167MHz.

## FrodoKEM on FPGA

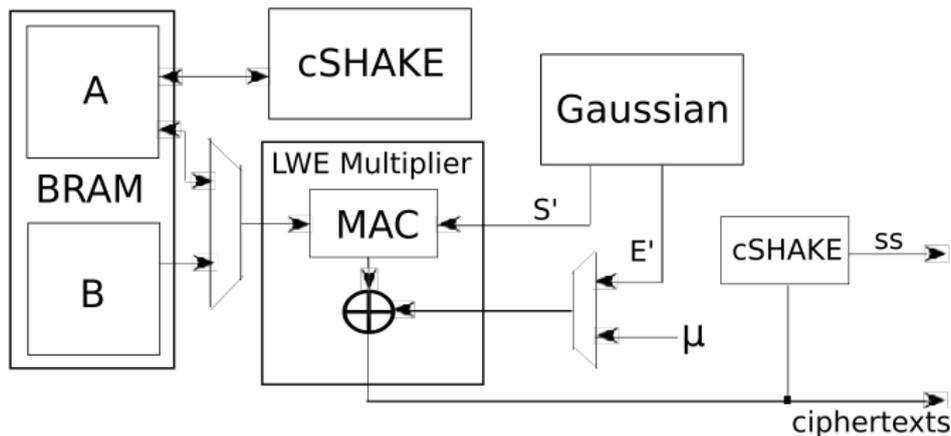


Figure: An overview of our FPGA design of FrodoKEM Encapsulation.

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## Results and Comparisons

- ✂ Competes with NewHope area consumption, but much slower performance.
- ✂ Huge savings in BRAM compared to LWE Encryption [HMO<sup>+</sup>16].

**Table:** FPGA consumption and performance of our proposed designs, benchmarked on Artix-7.

Cryptographic Operation	LUT/FF	Slice	DSP	BRAM	MHz	Ops/sec
FrodoKEM-640 Keypair	6621/3511	1845	1	6	167	51
FrodoKEM-640 Encaps	6745/3528	1855	1	11	167	51
FrodoKEM-640 Decaps	7220/3549	1992	1	16	162	49
FrodoKEM-976 Keypair	7155/3528	1981	1	8	167	22
FrodoKEM-976 Encaps	7209/3537	1985	1	16	167	22
FrodoKEM-976 Decaps	7773/3559	2158	1	24	162	21
cSHAKE*	2744/1685	766	0	0	172	1.2m
Error+AES Sampler*	1901/1140	756	0	0	184	184m
NewHopeUSENIX Server [OG17]	5142/4452	1708	2	4	125	731
NewHopeUSENIX Client [OG17]	4498/4635	1483	2	4	117	653
LWE Encryption [HMO <sup>+</sup> 16]	6078/4676	1811	1	73	125	1272

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## Conclusions

- ✂ We show that hardware significantly minimises the performance distance between standard and ideal lattice-based KEM, able to utilise less than 2000 slices and remain practical.
- ✂ Memory optimisations for microcontrollers show 66% savings vs reference design and 40% vs optimised PQM4 design.
- ✂ It would be interesting to see results for Frodo on FPGA with increased multipliers. As well as how it performs vs. other NIST PQC candidates.

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## Conclusions

- ✦ Our results show the efficiency of FrodoKEM and help to assess the practical performance of a possible future post-quantum standard.



Although rings are still good to use, unless you're Gollum...

Thank you for listening. Any questions?

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